

A SUITE OF MODELS FOR CPI FORECASTING

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Abstract

This paper reviews the suite of models the National Bank of Ukraine uses for short-term forecasting of CPI components. I examine the forecasting accuracy of the following econometric models: univariate models, VAR, FAVAR, Bayesian VAR models, and Error Correction models. The findings suggest that for almost all components there are models that outperform benchmark AR models. However, the best performing individual model at each horizon for each component differs. Combined forecasts obtained by averaging the models' forecasts produce acceptable and robust results. Specifically, the combined forecasts are most accurate for core inflation, while they can beat the AR benchmark more frequently than other types of models when it comes to the raw food price index. This study also describes relevant data restrictions in wartime, and highlights avenues for improving the current suite of models for CPI forecasting.

JEL Codes

C32, C51, C52

Keywords

short-term forecasting, CPI, forecast evaluation

Acknowledgments: I appreciate the valuable comments of my colleges from the National Bank of Ukraine, especially Anton Grui and Andriy Tsapin. I would like to thank the anonymous reviewer for providing me with the ideas on how to restructure the paper and make some issues more comprehensive. I also extend my gratitude to Massimiliano Marcellino, professor of Econometrics in the Economics Department of Bocconi University, for his useful comments.

1. INTRODUCTION

In 2016 the National Bank of Ukraine (NBU) instituted de facto an inflation targeting (IT) regime. Under this framework, producing accurate and well-grounded forecasts of inflation is a difficult but essential task for the successful implementation of monetary policy. Usually, structural and semi-structural models are applied for a medium-term forecast, which covers a two- to four-year time horizon, whereas for the short-term forecast a variety of econometric models are used. The medium-term orientation gives central banks the flexibility to respond in an appropriate manner to the different economic shocks that may occur, however short-term projections are also of great importance for policy makers since they serve as a starting point for medium-term forecasts and policy analysis.

The development of the set of models for short-term CPI forecasting at the NBU started at the end of 2016 as part of a plan for a well-tailored and structured FPAS (Forecasting and Policy Analysis System). The first types of models developed were simple AR models and an ECM model aimed at forecasting one of the main CPI components – the raw food price index (RFPI). In the course of time, new types of models were developed to forecast the components of core inflation. Namely, in 2021 the set of models for the RFPI and Core CPI consisted of the following types: univariate models (AR, ARMA), vector autoregressive (VAR) models, factor augmented VAR (FAVAR) models, Bayesian VAR (BVAR) models, and error correction models (ECM). These models take into account the peculiarities of the Ukrainian economy and are based on the experience of peer central banks. It is important to point out that the final forecast

combines the results of the model forecasts and expert judgments. Additionally, nowcasting based on web scraping is also used for the first month of the forecast. Detailed information regarding online price indexes which are used for nowcasting can be found in Faryna et al (2018).

The aim of this paper is to review the suite of econometric models used by the NBU for short-term CPI forecasting, examine the forecasting accuracy of these models, and elaborate recommendations on how to further improve the current models.

Various methods are usually applied for short-term inflation forecasting in central banks: starting from simple univariate models up to large dynamic factor models and Bayesian inference. Univariate models are a popular tool for producing bottom-up forecasts (Alvarez and Sanchez, 2017). Whereas multivariate models are able to incorporate a large amount of economic information into the short-term forecasting process (Akdogan et al., 2012). As a large amount of complex data is becoming available, increasing complexity in the data leads to increasing complexity in the models, with a growing number of parameters to estimate. One of the easiest ways to solve this issue would be to build a leading indicators model, either by regressing inflation on principal components derived from the indicators' data set, or to use each series individually and then combine forecasts. Dynamic factor models may be applied, as they not only benefit from exploiting information from large datasets but also account for the unbalanced data problem and have good forecasting properties. Another way to overcome dimensionality problems is to apply Bayesian techniques.

Several studies argue that in the presence of a large set of alternative forecasts, it is worth combining them rather than selecting one of them (Kapetanios et al. (2007) and Bjornland et al. (2008)). To verify the hypothesis that a combined forecast obtained by simply averaging all the alternative available forecasts tends to produce good and robust results in a variety of cases, I am going to compute combined forecasts and evaluate their accuracy.

The findings suggest that for almost all components there are models which outperform benchmark AR models. However, the best performing individual model differs at each horizon for each component. Combined forecasts obtained by averaging models' forecasts do produce good and robust results: for core inflation the combined forecasts are the most precise ones, while for the raw food price index they can beat AR benchmark more frequently than other types of models.

Due to data scarcity, especially for core components, a relatively short sample period for forecast evaluation is a considerable limitation. Moreover, the period of study covers the time of recovery from the financial crisis and military conflict, the switch to the IT regime in 2016, as well as COVID-19 pandemic. All these specific shocks may affect the behavior of macroeconomic variables and the relationships between them. That is why the research outcomes may be sensitive to the sample size, as well as the period studied.

To address the issue of IT-regime change, I estimate and analyze descriptive statistics for CPI components for "before IT" and "IT" subsamples. Two pre-IT samples were considered: one includes the whole period before 2016, while the alternative period excludes the beginning of 2015, the period when Ukraine experienced a huge nominal devaluation of the hryvnia. Note that there is not such a great difference in means if the devaluation period is omitted. This means that the difference was mainly explained by the effect of exchange rate pass-through to inflation. To solve the problem, I include the exchange rate as a control variable to multivariate models and include a dummy variable in univariate models.

For the COVID-19 crisis, I compare the percentages of types of models that have the best accuracy for various horizons and components for the whole sample of forecasting exercise and for the period of the COVID-19 pandemic. The results reveal that a different set of models are the most precise during COVID-19 pandemic times compared to the set for the whole forecasting sample. Namely, in crisis times models with a broad information set are more effective, and expert judgments may improve forecasts significantly.

This paper contributes to the existing literature by introducing a suite of models for short-term forecasting of inflation in Ukraine and analyzing their forecasting properties. The forecasts of inflation produced by this suite of models provide policy makers with a useful tool to assess current economic conditions and short-term developments.

The paper is organized as follows. In the next section techniques for short term inflation forecasting in CBs are examined. In section 3, the suite of models used for CPI forecasting at the NBU is described. The section contains both theoretical and empirical parts. In section 4, the forecasting properties of the models are reported and discussed. Finally, section 5 sets out conclusions and provides some recommendations on how to improve the forecasting performance of the models.

2. COMPARISON OF TECHNIQUES USED FOR CPI FORECASTING IN CENTRAL BANKS

Central banks usually apply a range of approaches and methods for short-term inflation forecasting. The following central banks are reviewed for their short-term forecasting methods: The Bank of Spain (BoS), the National Bank of Poland (NBP), the Central Bank of Bosnia and Herzegovina (CBBH), the Bank of England (BoE), the Central Bank of the Republic of Turkey (CBRT), the Bank of Norway (BoN), the Reserve Bank of New Zealand (RBNZ), the European Central Bank (ECB) and the Bank of France (BoF).

Information on the methods of the short-term inflation forecasting in these central banks, as well as the references, can be found in Table A.1, Appendix A.

The following conclusions can be drawn after reviewing the modeling techniques used by various central banks.

First, not all of the central banks focus on a model-based forecast of headline CPI. Some of them (BoS, BoN and CBRT) exclude food, energy or administrative prices (mostly prices on tobacco) from headline CPI because of the high volatility and poor predictability of these components. However, others argue that such an approach is not suitable for countries with a high share of these volatile groups (CBBH), as inflation excluding food and energy deviates significantly from the inflation faced by a typical household in the country. In most of the studies, the horizon of short-term forecasting varies from two to four quarters. The ECB has an even broader horizon of six quarters. RBNZ applies similar types of short-term forecasting models to those it uses for medium-term inflation forecasting as a cross-check for central forecasts, and thus has a forecasting horizon of eight quarters. The MAPI model of the BoF provides both monthly forecasts for 12 months, and quarterly forecasts for 12 quarters.

Second, all the reviewed banks use various types of models, starting from simple univariate models up to large dynamic factor models and Bayesian inference. Univariate models are a popular tool for producing bottom-up forecasts, but they are mostly applied when there is a high degree of disaggregation (for example, 120 components in BoS). Such a strategy enables more detailed information on each component to be incorporated into the forecast.

In contrast, the ECB and BoE use multivariate models to forecast a smaller amount of CPI components. Since there is a need to incorporate a large amount of economic information into the short-term forecasting process, in addition to standard VAR and single equation models, many central banks apply methods and approaches that can summarize the information contained in large datasets by reducing their dimensions (i.e. reducing the parameter space). The easiest way to proceed is to build leading indicator models (NBP, BoN) either by regressing inflation on principal components derived from the indicator data set, or to use each series individually and then combine forecasts. Dynamic factor models have also been increasingly popular at central banks (CBRT, NBP, BoN) as they not only benefit from exploiting information from large datasets, but also account for the unbalanced data problem (the so-called "ragged edge") and have good forecasting properties.

Another option for overcoming dimensionality problems is to apply Bayesian techniques. BVARs are used at the NBP,

CBRT, BoN, ECB, RBNZ, and CBBH. The main strength of Bayesian estimation is precisely the fact that it is able to supplement the information contained in the data with expert information. When producing a forecast, BVAR models use a very large panel of data without exhibiting any signs of overfitting, and, as reported in the examined working papers, they produce good forecasting results. In Bayesian analysis a correct prior specification is a very important part of model creation. Various types of priors are used at central banks: a theoretical Minnesota-style (CBRT, ECB, CBBH) or an uninformative, conjugate Normal-inverse Wishart (BoN).

Some central banks also use modifications of the Phillips curve in the forecasting process, as it is considered to be a canonical economic model for forecasting inflation. Namely, both BoS and NBP add a backward-looking element to the equation. NBP uses unit labor costs (a proxy for marginal cost) instead of the output gap. While CBRT estimates the Phillips curve in a time-varying fashion.

Third, since it is important to estimate and report the uncertainty around the forecasts, the majority of central banks mostly use density forecasts instead of point forecasts. Moreover, as all banks have a suite of models, the question arises as to whether it is necessary to combine forecasts or to identify a baseline model and to use the others as supplementary ones. In the BoN paper, it is strictly recommended to combine some forecasts: “the next generation of macro modelers at Inflation Targeting central banks should adapt a methodology from the weather forecasting literature known as “ensemble modelling.” The NBP, CBRT, BoS and BoN report that the combined forecasting performance is better than that of any single model. However, the forecasts are combined in different ways. The BoS and CBRT use RMSE-based weights, whereas NBP uses log-predictive scores inside the models’ groups, and equal weights across the groups. At BoN, the weights attached to different models change within the quarter as new data is released. Some banks (BoN, CBRT, RBNZ, NBP) apply the strategy of building large sets of models of a similar type and then combining the forecasts from each type of model. The motivation for this is to avoid instabilities in the models caused by considerable uncertainty regarding the models’ specifications (e.g. choosing lag lengths, data-samples, variables to be included, etc.).

Fourth, depending on the type of model, the forecasts can be conditional or unconditional. The conditional forecast is based on the assumed future path of a set of inflation determinants (i.e. assumptions). Hence, conditioning allows forecasts to be more realistic. It makes the interpretation of forecasts and story building around them easier. However, the assumed values of these factors may vary from the actual ones and compound the forecasting error.

Fifth, many central banks are reporting that BVAR models have superior forecasting abilities in comparison to other models (CBBH, CBRT, ECB). For inflation in Spain, the best model is the multivariate one. Namely, a transfer function model that consists of single equation models describing the relationship between the main components of inflation and various explanatory variables. In the CBRT paper, the authors argue that models that use multivariate predictors outperform univariate models in terms of forecasting inflation, since “multivariate models exploit larger data sets, which are likely to contain more information about inflation, compared to univariate models.” In contrast, for inflation in Norway, the leading indicators model class shows the

best performance most of the time, for all horizons. Thus, for BoN having a broad information set seems to add little extra value to performance. As for Phillips curve models, in general they tend to show poorer forecasting performance in comparison to other models, however they can provide some helpful insight as they seek to identify the effect on inflation of changes in demand.

To sum up, the NBU applies similar methods and techniques for short-term inflation forecasting as at peer central banks. As various banks use different measures of accuracy, and look at various forecast horizons and price indexes (CPI or different components of CPI), it is not possible to compare quantitatively the precision of the NBU forecasts to those at peer central banks. However, it is possible to compare whether the same techniques are claimed to be superior, and examine the issue of the accuracy of combined forecasts.

3. CPI FORECASTING IN UKRAINE

3.1. Stylized Facts of CPI

In the last two decades, inflation in Ukraine has been relatively high, the average year-over-year growth being around 10%. Since 2005, Ukraine has had two episodes with inflation exceeding 20%. In 2008, at the beginning of the World Financial Crisis, the Ukrainian economy was overheated. Despite the slowdown in GDP growth during the crisis, consumption growth together with a loose fiscal policy aimed at increasing social standards resulted in a substantial growth in minimum wages, which pushed prices upward.

During the Great Recession, Ukraine was hit by a sharp terms-of-trade shock: the prices of steel (in 2008 steel represented about 40% of exports and 15% of GDP) declined substantially, while energy import prices remained high due to the phasing out of Russia’s gas subsidies. The terms of trade shock had a considerable impact on the real sector. However, major strains were already showing in the banking system following a system-wide run on deposits. A loss of confidence domestically led to capital flight from the hryvnia into foreign exchange cash. Altogether, this led to a massive devaluation of the currency, a fall in real GDP, and a shrinking of the current account deficit in 2009.

In 2010-2011 the economy started recovering. Inflation fell to single digits and the exchange rate stabilized, while growth in consumption and nominal wages rebounded.

In 2012-2013 inflation approached zero due to weak economic activity (the annual GDP growth was 0.2-0.0%). Keeping the exchange rate stable led to an accumulation of huge imbalances in the economy. In 2014 these imbalances, along with the military conflict in the east of the country, led to a severe economic crisis with the real GDP falling by 10% in 2015, a sharp depreciation of the hryvnia, and inflation reaching a peak of almost 60% year-over-year in the spring of 2015. It is worth noting that the natures of the two episodes of high inflation (2008 and 2015) are different: the second inflationary spike was caused by the pass-through of the hryvnia devaluation, whereas in 2008 rising inflation was a sign that the economy had been overheating.

In August 2015 the NBU announced a transition to an IT regime in order to break the upward inflationary trend and stabilize the economy. De facto it moved to an inflation targeting regime in 2016, setting the following targets for inflation:

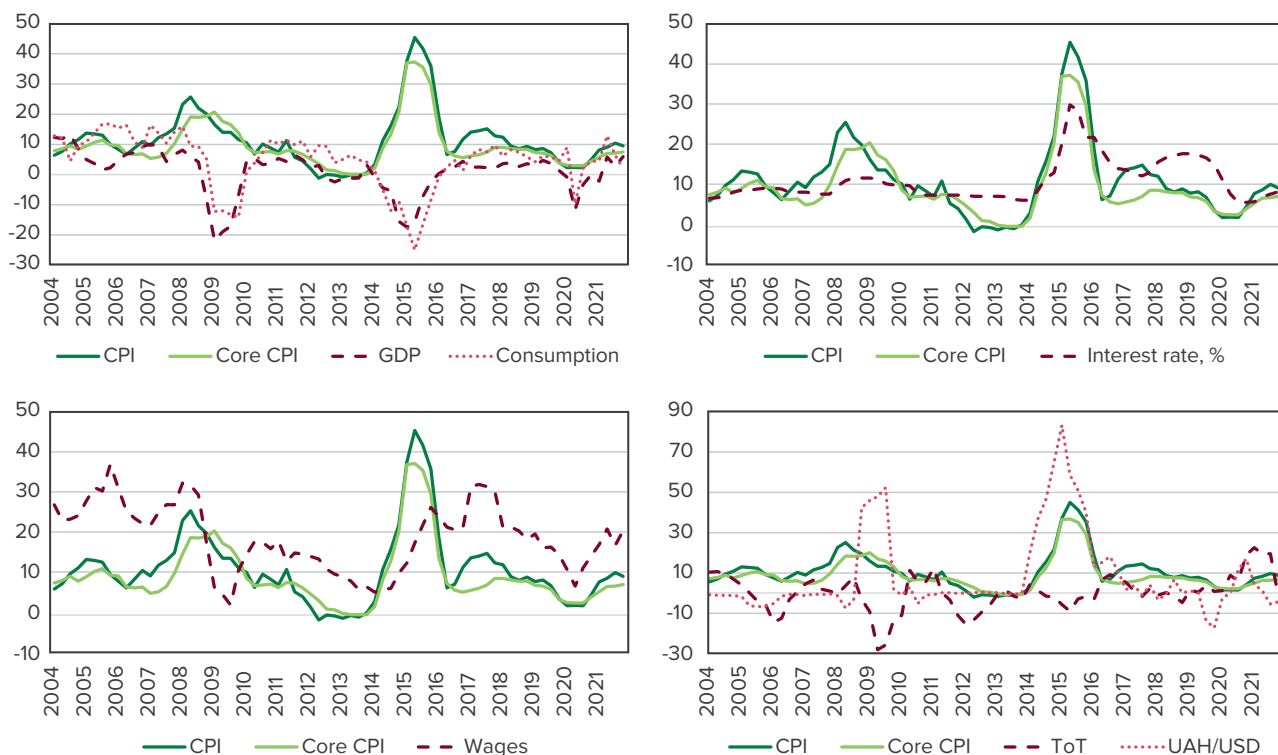


Figure 1. Main Economic Indicators, yoy in logs

- 12% +/- 3 ppts as of the end of 2016;
- 8% ± 2 ppts as of the end of 2017;
- 6% ± 2 ppts as of the end of 2018;
- 5% ± 1 ppt as of the end of 2019 and further on.

The inflation targeting regime uses the short-term interest rate as its main instrument, and foreign exchange interventions as an additional one. To bring inflation down to the target, the NBU increases the interest rate to moderate demand and ease inflationary pressures. Thus, a gradual strategy of bringing inflation to its target was chosen deliberately in order to minimize the costs of disinflation for economic growth.

In general, the process of disinflation that started in 2016 went well, and in 2019 consumer price inflation gradually declined to a six-year low of 4.1%. Thus, the NBU finally achieved its target of 5% ± 1 ppt. The average GDP growth was 2.8% in 2016-2019.

2020 brought a new challenge: The COVID-19 pandemic was a shock of unprecedented severity affecting all areas of the economy. At the beginning of the COVID-19 pandemic, households' consumer behavior changed. In the first half of 2020, during the stricter lockdown, some goods and services were not consumed, as selling them was prohibited or restricted. Thus, households cut spending on these items. The ability to work remotely affected demand for clothing and transportation services. Plummeting demand for many non-essential goods and services caused a decrease in prices. Prices for fuel also decreased significantly due to weak demand. However, prices for some raw food components increased substantially, due to both a lower-than-expected harvest and higher prices for food on the international markets.

Moreover, the structure of consumer spending was impacted by physical restrictions on the consumption of some goods and services, changes in demand on the back

of the spread of remote working and studying, and high uncertainty over the course of the pandemic. The changes in consumer patterns during COVID-19 may not be fully reflected in official CPI estimates because according to "Consumer Price Index Manual: Theory and Practice" (2004), the stability of the price index weight structure has to be preserved. The NBU estimated a new price index with adjusted CPI weight structure¹ to analyze the impact of changes in consumption. According to NBU estimates of Covid inflation, by the end of 2020 it exceeded official inflation by 0.2–0.6 ppt. This corresponds in general to the results obtained by other countries. Moreover, considering the statistical properties of the CPI (see the means and deviations of the CPI components in Figure 2) such a deviation from official inflation probably doesn't affect the forecasting accuracy of the models significantly. In general, being lower than its target during 2020, inflation returned to its target in December 2020. However, in 2021 consumer inflation accelerated and exceeded its target largely due to rises in the prices of energy and some raw food items.

To sum up, the recent economic developments in Ukraine show that along with domestic conditions, external prices and the exchange rate are other important drivers of inflation and should be taken into account when forecasting Ukrainian inflation.

3.2. Factors Influencing The Dynamics of CPI Components

The NBU uses the year-over-year growth rate of CPI index as its target. CPI tracks changes in the market prices of a basket of consumer goods and services. It is comprised of 328 sub-indices. The weights of the items

¹ More information on estimates of COVID-19 inflation can be found Box 1. Covid Inflation in Ukraine from the NBU Inflation Report (January, 2021).

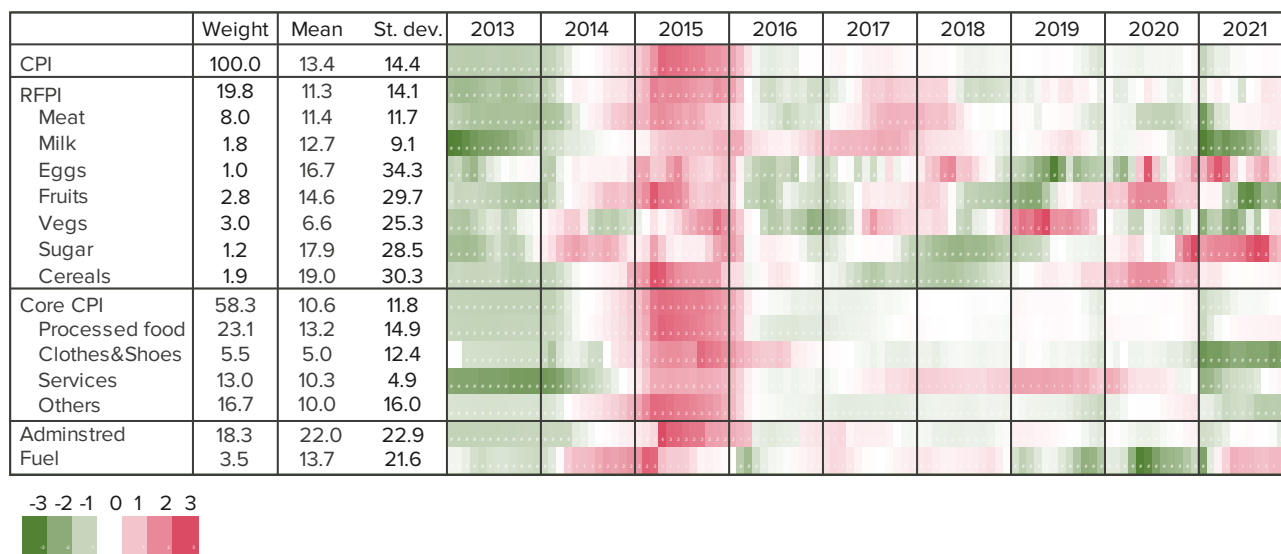


Figure 2. Heat Map of CPI Components

Note: Heat map is constructed for year-over-year, end of period percent change of CPI components, all indices are normalized. Weights are average for 2016-2021, means and standard deviations are calculated for 2013-2021.

from the basket are dynamic and can be adjusted to changes in the structure of consumption and in the type of items consumed.

The dynamic of sub-indices is not homogeneous. There are many indices, and their underlying characteristics vary widely in terms of both mean and standard deviation. One of the ways to simplify the analysis of these time series is to use a heat map that visually represents the relative inflation levels of various CPI components (as in McGillicuddy and Ricketts (2015) and Álvarez and Sánchez (2017)). Heat maps for some sub-indices of Ukrainian CPI are presented in Figure 2 (a more detailed heat map containing 92 items is presented in Figure B.1, Appendix B). It can be seen that for different CPI components, the periods of increase or decrease in prices as well as the causes of such dynamics are non-identical. For example, in mid-2020 only fuel prices decreased substantially as a consequence of a slump in global oil prices. In 2019, the increase in the prices of services was caused by a change in tariffs for transportation and communications, whereas an increase in prices on vegetables was spurred by unfavorable weather conditions. Such examples show that altogether with the analysis of common factors influencing inflation, it is worth splitting CPI into groups and looking at the factors which are specific for each group. will look into four major components of the CPI: core CPI, the raw food price index (RFPI), prices for fuel, and administrative prices.

RFPI (Raw food price index)

The RFPI accounts for 19.8% of the CPI basket. The RFPI itself consists of the following components: “meat”, “milk”, “eggs”, “cereals”, “fruits”, “vegetables” and “sugar” (see the price dynamic of the components in Figure 3). The RFPI is considered to be the most volatile component of CPI for several reasons. First, raw food goods are demand inelastic, i.e., a consumer cannot eat twice as much food just because the price for that food has decreased substantially. Second, a quick adjustment to a supply shock in the short run is also difficult task, i.e., crop and livestock production are influenced by weather and diseases. If a crop is destroyed by severe weather conditions, it takes time to grow a new one.

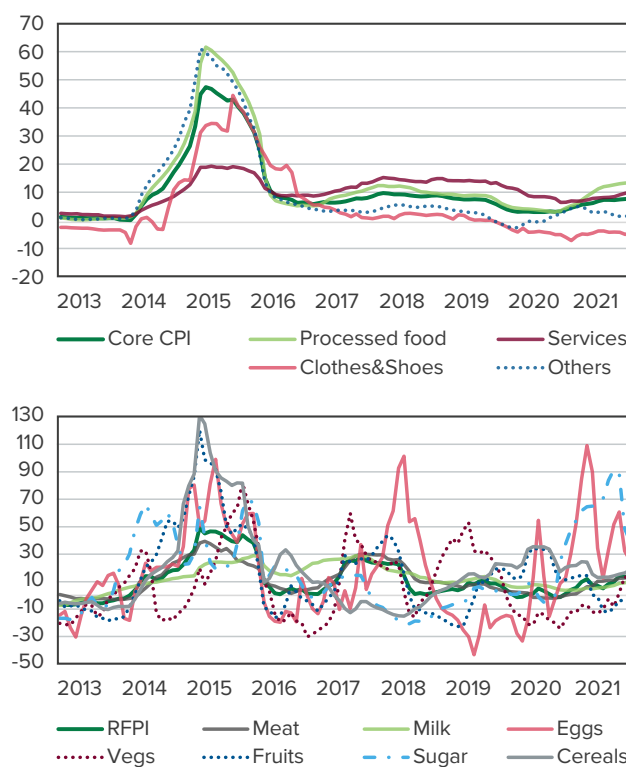


Figure 3. The Dynamics of Sub-Components of CPI, 12-mnths percent change

The RFPI is driven more by supply than demand factors – production and harvest are important determinants of the RFPI dynamics. In order to decide which factors should be taken into account, i.e., which sub-components depend not only on harvest or production, but also on the exchange rate and prices on international markets, it is worth analyzing consumption balances – namely the share of exports in production and the share of imports in consumption. A full set of plots can be found in Figure B.2, Appendix B. In general, it is obvious from the consumption balances plots that for the “cereals”, “meat”, “milk” and “fruits” groups, external factors are important. As there is a trend for increasing exports of

eggs and sugar, the exchange rate and prices on external markets could be considered for these groups of goods as well.

It is worth mentioning that seasonality in food items is more profound than in other items, and that this also depends on the share of domestic production in consumption (e.g., potato and vegetables are planted and consumed mostly domestically and have more intense seasonality than meat, which is traded internationally) and shelf life (the seasonality of the “processed food” group is less profound than that of the RFPi).

Core CPI

Core CPI accounts for 58% of the CPI basket and consists of four main components: “processed food”, “clothes and shoes”, “services” and “others”.

As Ukraine has moved to an inflation targeting regime, it stands to reason that the policy rate should have an influence on the least volatile and most monetary policy relevant part of the CPI. However, taking into account the medium-term orientation of monetary policy and the fact that I am focused on short-term forecasting, it is also worth considering other indicators that are more applicable for the short-run.

As core inflation is considered to be more demand driven, the nominal wage indicator seems to be a good proxy for changes in demand, given that it is available on a monthly basis and assumptions regarding its dynamics during the forecasting period are also available.

Exchange rate dynamics seem to be another important factor: when the devaluation occurred in 2015 the “processed food” and “others” groups had the highest exchange rate pass-through (these groups have more intense color on the heat map in 2015). The main reason for such behavior is probably the high share of imported groups in these two components. In contrast, “services” had the smallest pass-through, reflecting the high share of non-tradable goods in this group.

Fuel Prices

Fuel prices account for 4% of the CPI basket. Fuel prices in domestic currency mostly depend on the nominal exchange rate and oil prices on international markets, as Ukraine is considered to be a net importer of energy goods. The prices for fuel are not forecasted within the framework of time series models, and need only assumptions for the nominal exchange rate, oil prices on international markets, and the excise tax.

Administered Prices

Administered prices account for 18% of the CPI basket. They mainly consist of prices for utilities, transportation services and alcohol and tobacco. As the dynamics of these prices mostly depend on information about the value of excise tax and information from local authorities regarding tariffs, it would be reasonable to use expert judgments instead of time series models when forecasting these prices.

To sum up, headline CPI is broken down into smaller components, each representing a different subset of goods and services. The suite of models is applied for two components

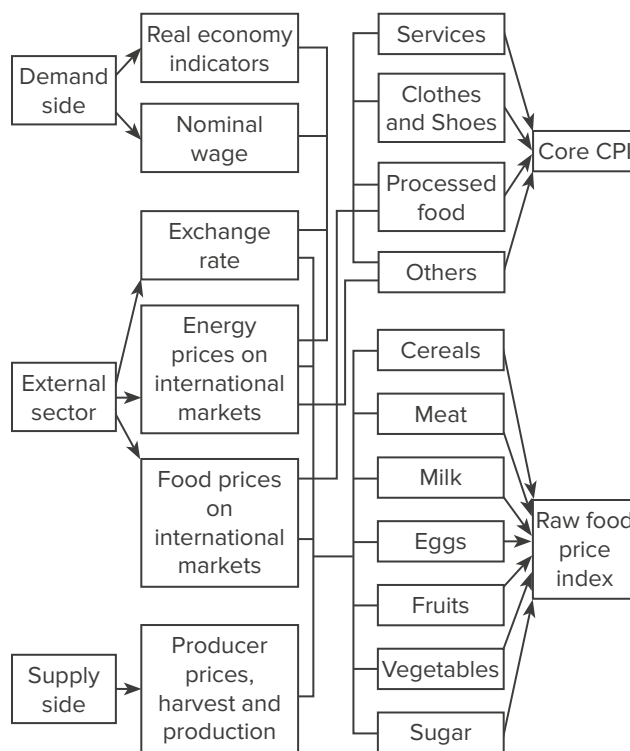


Figure 4. Factors that Drive the Dynamic of CPI Components

of CPI, namely, the RFPi and core CPI. Altogether they account for 78% of headline CPI. On the basis of the analysis conducted above, the indicators used in modelling are represented in Figure 4. More detailed information about the time series² used in the models is given in Tables A.1-A.2, Appendix A.

3.3. The Suite of Models used by the NBU

The NBU uses several types of models for the short-term forecasting of inflation in Ukraine: univariate models (AR, ARMA), vector autoregressive (VAR) models, factor augmented VAR (FAVAR) models, Bayesian VAR (BVAR) models, and error correction models (ECM). Each type is introduced and discussed below.

But before discussing the different types of models for the short-term forecasting of inflation, I would like to address the issue of sample stability. First, instability may arise due to a switch in the monetary policy regime. Namely, the implementation of the IT regime in 2016 could have changed the statistical properties of data, which can lead to huge forecasting errors if forecasts of price indices after 2016 are produced by models estimated using data from before 2016. To verify whether the statistical properties have changed, the means, standard deviations and AR coefficients of RFPi and Core inflation are analyzed (see Figure B.3). Two pre-IT samples were considered: one includes the whole period before 2016, and the other excludes the beginning of 2015, when Ukraine experienced a huge nominal devaluation of the hryvnia. We can see in the figure that if we do not consider the devaluation period, there is not such a great difference in means, indicating that the difference was mainly caused by the

² All data are measured in natural logarithms. As almost all levels of prices, production and harvest are I(1) processes according to the stationarity test, first differences of the variables are used. An identifiable seasonality test is used to decide whether a variable is to be seasonally adjusted by X12.

effect of exchange rate pass-through to inflation. To solve the problem, multivariate models contain the exchange rate as a regressor. Whereas for univariate models, a possible solution is the inclusion of dummy variables (as described in the ARMA models subsection below). It is clearly seen that during the IT period the values of the standard deviation for RFPI and Core inflation decreased, which is quite a common situation for countries implementing an IT regime. See, for example, how inflation deviation shrank after the implementation of the IT regime in New Zealand (Archer, 2000).

Second, sample instability may be caused by various factors that are specific to a certain group of goods. For example, changes in consumption or production patterns (an increase in the share of imports in consumption or exports in production) may influence the coefficients of a model. Similarly, dummies can be used to take these changes into account.

Autoregressive (AR) Models

Time series models, which in general extrapolate patterns in historical data, are considered to be the most appropriate for short-term forecasting (Galbraith and Tkacz (2006)). Univariate models, the simplest among them, are commonly used as a benchmark in the forecasting literature. Quite often, the forecasting properties of these models are found to be superior to large multiple-equation models such as vector autoregression and traditional structural macroeconomic models. Moreover, having few independent variables, they are believed to be convenient for short data samples.

Simple AR equations are estimated and used for forecasting. Lag length may be chosen according to various criteria (Akaike, Schwarz, Hannan-Quinn), however a first-order autoregressive model usually serves as a benchmark model.

AR equation can be written as:

$$dP_t^j = \alpha_0^j + \sum_{i=1}^l \alpha_i^j \cdot dP_{t-i}^j + \varepsilon_t^j \quad (1)$$

where P_t^j is a price level of j-component ³ at time t , dP_t^j is a first difference at time t , l^j is a l period lag, and ε_t^j is a randomly distributed error term.

AR equations are used both for forecasting the RFPI and core CPI components. The Schwarz criterion is used to find optimal lags. The results of the estimation are presented in details in Table A.4, Appendix A. The results show that the components of core inflation have more persistence than most components of the RFPI. This confirms the initial observation from the stylized facts section that the prices of most of raw food items are highly volatile. Moreover, some equations have quite a high S.E. (Standard Error) value. In other words, this type of model is not good at explaining the dynamics of certain prices. The results may be improved by using more sophisticated model structures, namely ARMA models.

Autoregressive Moving Average (ARMA) models

Another time series method for explaining variables in terms of their own past values is the ARMA (or more

generally ARIMA⁴) model. In addition to autoregressive terms, this model has moving average terms. The notation ARMA (l^j, q^j) refers to a model with l^j autoregressive terms and q^j moving-average terms for each j-th price component:

$$dP_t^j = \alpha_0^j + \sum_{i=1}^{l^j} \alpha_i^j \cdot dP_{t-i}^j + \sum_{k=1}^{q^j} \beta_k^j \cdot \varepsilon_{t-k}^j + \varepsilon_t^j \quad (2)$$

According to Box et al (2015), models containing processes of different types are considered to be more parsimonious. Namely, a model with small values l^j of and q^j will do as well at explaining a process dP_t^j as a high order AR(l^j) or MA(q^j) process.

ARMA models are used to produce disaggregated forecasts of core inflation components (240 items). To account for excessive market movements and possible structural changes, an ARMAX type of model (ARMA with exogenous variables) was chosen. Namely, dummy variables were added into the specification:

$$dP_t^j = \alpha_0^j + \sum_{i=1}^{l^j} \alpha_i^j \cdot dP_{t-i}^j + \sum_{k=1}^{q^j} \beta_k^j \cdot \varepsilon_{t-k}^j + \gamma^j * D_t^j + \varepsilon_t^j \quad (3)$$

where D_t^j is a dummy variable for j-th price component.

More detailed information about the model's structure and selection of dummy variables can be found in Krukovets and Verchenko (2019).

The main disadvantage of applying univariate models is that they do not use additional information that the available data may contain. In other words, such models don't reflect any structural relationships in the data, and lack economic meaningfulness. Thus, it is worth applying multivariate models to take into consideration additional information and increase the explanatory power of the model.

Vector Autoregressive (VAR) Models

VAR models are usually applied to describe relationships between different variables as well as between current and lagged observations. A standard VAR with l lags is expressed as:

$$Y_t = A_0 + \sum_{i=1}^l A_i * Y_{t-i} + \varepsilon_t \quad (4)$$

where $Y_t = [y_{1,t}, \dots, y_{n,t}]^T$ is a vector of variables, A_0 is a $n \times 1$ vector of constants, A_i is a $n \times n$ matrix of coefficients of Y_{t-i} , l- is number of lags and ε_t is a $n \times 1$ vector of residuals with multivariate normal distribution $\varepsilon_t \sim N(0, \Sigma)$, $E(\varepsilon_t \varepsilon_t') = \Sigma$, $E(\varepsilon_t \varepsilon_s') = 0$ if $t \neq s$.

Many empirical studies on the international transmission of shocks are based on VAR models that include only a few selected variables. However, Mumtaz and Surico (2009) argue that because of their small-scale, there may be a possibility of mis-specification of the models or incorrect interpretation of fundamental shocks. From a practical perspective, small scale VARs are also unable to provide inferences on a large number of variables that may be of

³ The number of components is J, j=1...J, in our case J=11, namely 7 components of RFPI and 4 components of Core CPI.

⁴ An ARIMA (autoregressive integrated moving average) model is a generalization of an ARMA model. ARIMA models are used when data show evidence of being non-stationarity. To eliminate non-stationarity, differencing is applied (as many times as an order of integration of the initial series). Since we model month-over-month changes in prices, which are supposed to be stationary, we do not need differencing. For ARMA models J=240.

interest. Hence, for the purposes of short-term forecasting, a wider information set can be used.

Though large VAR models disclose more information from data and are commonly used in forecasting, estimation of the parameters of such models requires long data samples, as the number of VAR parameters increases with the square of the number of variables. I.e., the number of observations must exceed the number of estimated parameters, which means being more than $k = n(n * l)$ for model (4).

One way to avoid the dimensionality problem, if the variable of interest is $y^j_{1,t}$ is to estimate $n^j - 1$ bivariate VARs of the form, as in Andersson and Löf (2007):

$$Y^j_{b,t} = A^j_{b,0} + \sum_{i=1}^l A^j_{b,i} * Y^j_{b,t-i} + \varepsilon^j_{b,t}, b = 1 \dots n^j - 1 \quad (5)$$

where $Y^j_{b,t} = [y^j_{1,t}, y^j_{b+1,t}]^T$, $y^j_{1,t} = dP^j_t$, $y_{b+1,t}$ is the first difference of the b+1-th variable

At the end, each of models will produce forecasts for P^j_t . Thus, having $n^j - 1$ individual forecasts allows us to compute a variety of statistics and produce density forecasts for the variable of interest.

Bivariate VARs are estimated for seven components of the RFPI and four components of core CPI. The information set for each forecasted variable is given in Table A.5, Appendix A. Equal weights are used to construct a combined forecast for a set of bivariate VARs for each forecasted variable.

Another way to decrease dimensionality is to condense data in many variables into just a few variables, using factor analysis.

Factor Augmented VAR (FAVAR) Models

Bernanke et al. (2004) suggested adding an unobserved factor into a small-scale VAR model. Earlier, Stock and Watson (2002) forecasted inflation using factor estimation to account for more than several hundred variables. Further details regarding the optimal number of dynamic factors and tests for the factor restrictions can be found in Stock and Watson (2005). In our case, the model is similar to that in Lombardi et al (2012), who examined linkages across non-energy commodity price developments using a FAVAR model:

$$\begin{bmatrix} Y_t \\ F_t \end{bmatrix} = \Phi(L) \begin{bmatrix} Y_{t-1} \\ F_{t-1} \end{bmatrix} + u_t \quad (6)$$

where $Y_t = [y_{1,t}, \dots, y_{m1,t}]^T$ is a vector containing the variable of interest and some fundamentals, $F_t = [f_{1,t}, \dots, f_{m2,t}]^T$ – factors extracted from information set $X_t = [x_{1,t}, \dots, x_{n,t}]^T$, $m1 + m2 \ll n$, u_t is a $(m1 + m2) \times 1$ vector of residuals with multivariate normal distribution $u_t \sim N(0, Q)$.

There are several options for extracting factors for FAVARs. Since Bernanke et al. (2004) and Oskarsson and Lin (2018) found that applying more sophisticated methods rather than simple principal components analysis (PCA) did not yield significantly better results, I am going to use PCA as well.⁵

FAVARs estimated for seven components of the RFPI and four components of core inflation have similar bivariate structure to the models from the previous section. Namely, for j-th price component:

$$Y^j_{favar,t} = A^j_{favar,0} + \sum_{i=1}^{l^j_{favar}} A^j_{favar,i} * Y^j_{favar,t-i} + \varepsilon^j_{favar,t} \quad (7)$$

where $Y^j_{favar,t} = [y^j_{1,t}, pc^j_{1,t}]^T$, $pc^j_{1,t}$ is the first principal component of the data set $[y^j_{2,t}, \dots, y^j_{n,t}]$ which are the first differences of the variables and $y^j_{1,t} = dP^j_t$ is the forecasted variable. The information set for each component is similar to that used for bivariate VARs (see Table A.5, Appendix A). As mentioned, only the first principal component, which explains the most, was used. However, for some CPI components it is obvious that it is not sufficient to have only the first principal component.

So far, most of the described approaches did not consider models with exogenous variables. Hence, they do not require any assumptions on factors which allow a wider information set to be used.

However, it is also worth having models containing exogenous variables. Usually, forecasts are based on some assumptions about either external or internal factors (e.g., for the RFPI index it may be information regarding harvests or world prices dynamics, for core CPI – an increase in minimum wages announced by the government). Consequently, making forecasts based on assumptions allows the forecasts to be more realistic and consistent, as well as it making the interpretation of forecasts and building a story around them easier. Moreover, these models may provide us with a scenario analysis.

Bayesian VAR (BVAR) Model

Another alternative for dealing with the dimensionality problem by shrinking the parameters via the imposition of priors is a Bayesian VAR (BVAR) model. Given the fact that the sample size for the Ukrainian data is short, standard OLS estimates of parameters can be imprecise, thus making obtained impulse responses and forecasts unreliable. Banbura et al. (2008) show that with Bayesian shrinkage, it is possible to handle an unrestricted VAR with a large number of variables, where the data set can even be extended to incorporate disaggregated sectoral or geographical indicators.

The imposition of priors not only solves the dimensionality problem but supplements the information contained in the data with personal judgments contained in the prior. The recent literature on forecasting models points out that among a variety of empirical models, BVARs have superior abilities in forecasting.

One of the main challenges in this approach is the selection of prior distributions. I use the procedure developed in Litterman (1986) and impose Minnesota-style priors.

Let's consider a VAR with exogenous variables of the form of:

$$Y_t = \sum_{i=1}^l A_i * Y_{t-i} + C * X_t + \varepsilon_t \quad (8)$$

where $Y_t = [y_{1,t}, \dots, y_{n,t}]^T$ is a vector of variables, A_i is a $n \times n$ matrix of coefficients of Y_{t-i} , l – is the number of lags, C is a $n \times m$ matrix, $X_t = [x_{1,t}, \dots, x_{m,t}]^T$ is a $m \times 1$ vector of exogenous variables, and ε_t is a $n \times 1$ vector of residuals with multivariate normal distribution $\varepsilon_t \sim N(0, \Sigma)$, $E(\varepsilon_t \varepsilon'_t) = \Sigma$, $E(\varepsilon_t \varepsilon'_s) = 0$ if $t \neq s$

Reformulating the model for the whole data set [1...T] and vectorizing it we obtain:

⁵ FAVAR models are also used to nowcast quarterly GDP figures. More detailed information can be found in Grui and Lysenko (2017).

$$y^{vec} = \bar{X}\beta + \varepsilon^{vec} \tag{9}$$

where $y^{vec} = vec(Y)$, $Y = (Y_1, \dots, Y_T)'$

$$\bar{X} = I_n \otimes X, \quad X = \begin{pmatrix} Y_0 & \dots & Y_{1-l} & X_1 \\ \dots & \dots & \dots & \dots \\ Y_{T-1} & \dots & Y_{T-l} & X_T \end{pmatrix}$$

$$\beta = vec(B), B = (A_1, \dots, A_l, C)'$$

$$\varepsilon^{vec} = vec(E) \quad E = (\varepsilon_1, \dots, \varepsilon_T)', \varepsilon^{vec} \sim N(0, \bar{\Sigma})$$

where $\bar{\Sigma} = I_T \otimes \Sigma$

multivariate normal assumption on ε_t gives:

$$(y^{vec} | \beta) \sim N((X \otimes I_T)\beta, I_T \otimes \Sigma) \tag{10}$$

Bayesian estimation of VAR centers around the derivation of posterior distributions of β and Σ . It is assumed that β follows a multivariate normal distribution, with mean β_0 and covariance Ω_0

$$\beta \sim N(\beta_0, \Omega_0) \tag{11}$$

Litterman (1986) proposed the following prior: As most observed macroeconomic variables seem to be characterized by a unit root, each endogenous variable included in the model presents a unit root in its own first lags, and coefficients equal to zero for further lags and cross-variable lag coefficients. In the absence of prior belief about exogenous variables, the most reasonable strategy is to assume that they are neutral with respect to the endogenous variables, and hence that their coefficients are equal to zero as well. In the case of variables known to be stationary, this unit root hypothesis may not be suitable, so that a value around 0.8 may be preferred to a value of 1.

Ω_0 is assumed to be a diagonal matrix. The diagonal elements, corresponding to endogenous i and j at lag l are specified by:

$$\delta_{0,i,j}^l = \begin{cases} \left(\frac{\lambda_1}{l^{\lambda_3}}\right)^2 & \text{for } j = i \\ \left(\frac{\lambda_1 \lambda_2 \delta_i}{l^{\lambda_3} \delta_j}\right)^2 & \text{for } j \neq i \end{cases} \tag{12}$$

where $\lambda_1 \lambda_2$ and λ_3 are hyper-parameters and δ_i is the square root of the corresponding $(i, i)^{th}$ element of an initial estimate of Σ . The Minnesota prior also assumes that Σ is fixed, forming no prior on Σ .

More technical details can be found in Dieppe et al. (2016).

The procedure for the selection of the models for the RFPI and Core CPI that have the best fit is organized in a following way:

- 1) Various exogenous variables are tried, the ones with minimum log likelihood are chosen;
- 2) Standard lag length criteria were used to select the lag length (see Table A.6, Appendix A);
- 3) A grid search similar to the procedure used by Giannone et al. (2012) is applied to find the values of the hyperparameters for the model (see Table A.7, Appendix A).

The best specifications are presented in Table A.8, Appendix A.

For the RFPI components, the best model contains the exchange rate and the FAO price index as exogenous

variables.⁶ The magnitude of the exchange rate and FAO price index shock varies and, in most cases, depends on the share of exports in domestic production.

The impulse responses for the BVAR model with four components showed that a shock to “processed food” prices is significant for “others” prices. As both groups have a high share of imported goods, it is probable that the price dynamics of both “others” and “processed food” are driven by a common factor – exchange rate movements. To check this hypothesis, “processed food” and “others” prices were combined in one group and a BVAR for three components was estimated. Overall, the response of price index of combined groups to the exchange rate turned out to be significant. In addition, a model with three components is more parsimonious than one with four components.

The best models for core inflation components contain two exogenous variables – nominal wages and the exchange rate. The impulse responses show that prices in the “services” group are highly sensitive to nominal wages, while “processed food” and “others” prices are mostly affected by exchange rate dynamics. This conclusion is in line with the fact that prices for “services” contain a significant share of nontradables, and are mostly driven by domestic factors. As already mentioned, “others” and “processed food” prices have high share of imported goods, and as a consequence have the strongest response to exchange rate shocks.

Similarly to the BVAR for RFPI components, the exogenous variables of the BVAR models for Core CPI components were tested for exogeneity using a Granger causality test. According to the test results, the direction of causality for the exchange rate was as expected: from the exchange rate to the price components. In contrast, the “services” component and “others” component doesn’t have causality with nominal wages in either direction. Thus, treating nominal wages as exogenous may lead to the fact that the model won’t be able to interpret or will misinterpret some relationships between the variables.

The latter issue deserves being explored in a separate study. There are two possible options: either endogenize nominal wages, or find another more relevant exogenous indicator. In case of endogenizing nominal wages, the model forecasts should be conditioned on the indicator for nominal wages in order to be coherent with the forecasts for nominal wages produced during the forecasting cycle.

Error Correction Models (ECM)

If one wants to take into consideration specific factors for each component, systems of equations can be used. For example, in the case of the RFPI components, a more detailed analysis of supply factors would be interesting: instead of combined data on harvests, it is worth looking at the relations between an RFPI component and its particular harvest (e.g., how the harvest of vegetables and potatoes influences prices for vegetables and potatoes).

Also, while analyzing the influence of the exchange rate and external prices, it is worth having the advantage of being able to incorporate both short-run dynamics and long-run equilibrium relations among variables. Thus, in addition to existing models, an ECM (error correction mechanism)

⁶ To make sure that the FAO price index and the exchange rate can be treated as exogenous, a Granger causality test was conducted, indicating the correct direction of causality for exogenous versus endogenous variables.

model is estimated. A similar approach is applied in De Charsonville et al. (2017) to forecast the main components of HICP for France.

In an ECM type model, equations in levels represent cointegrating relationships⁷, which capture medium term dynamics, while the cointegration term derived from the equation accounts for the deviation of variables in the medium term. This approach thus provides us with a forecast of CPI components for both the short and medium term.

j-th equation in levels is the following:

$$P_t^j = \sum_{i=1}^{m^j} \theta_i^j \cdot X_{i,t}^j + \delta_t^j \quad (13)$$

where P_t^j is a price level of the j-th component $X_1^j \dots X_{m^j}^j$ – is a set of exogenous regressors for j-th price level, both price level and exogenous regressors are of I(1), and δ_t^j is a normally distributed residual.

To derive the coi_t^j term, rewrite (13):

$$coi_t^j = (P_t^j - \sum_{i=1}^{m^j} \theta_i^j \cdot X_{i,t}^j) = \delta_t^j \quad (14)$$

The equations in first differences contain the coi term (14):

$$dP_t^j = \sum_{i=1}^{m^j} \alpha_i^j \cdot dP_{t-i}^j + \beta^j \cdot coi_{t-1}^j + \sum_{k=1}^{n^j} \gamma_k^j \cdot dX_{k,t}^j + \varepsilon_t^j \quad (15)$$

where dP_t^j is first difference of the j-th price level, $dX_1^j \dots dX_{n^j}^j$ is a set of first differences of exogenous regressors $X_1^j \dots X_{n^j}^j$ for the j-th equation, and $\varepsilon_{i,t}^j$ is a normally distributed residual. Note that the set of exogenous variables for the j-th equation ($X_1^j \dots X_{m^j}^j$) in levels doesn't necessarily coincide with the set of exogenous variables for the j-th equation ($dX_1^j \dots dX_{n^j}^j$) in differences.

The model for core inflation consists of:

- 4 equations for core CPI components (as in 15)
- 4 identities for coi terms (as in 14), where coefficients are estimated using equations in levels (as in 13)
- Identity for aggregated index

Non-zero residuals are used to adjust the forecasted value of the current month (according to nowcasting results) as well as to include expert judgments into the model. The model for the RFPI has the same structure, although it consists of seven components.

To account for specific structural breaks, individual dummies are used. Namely, this reflects a growing export share in production (“meat”, “eggs”, “processed food”), import share in consumption (“vegetables”, “milk”), an asymmetric effect of currency appreciation (“cereals”), a surge in the minimum wage (“services”), pandemic events (“services”, “clothes and shoes”). Also, I look at coefficients’ recursive estimates to ensure the stability of the models’ parameters.

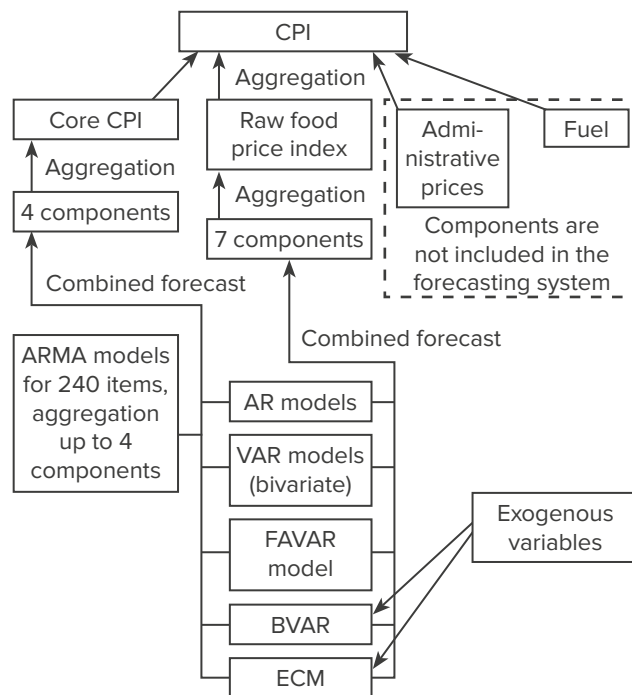


Figure 5. System for Short Term Forecasting of CPI

Additionally, I looked for various indicators that could be included into equations of Core CPI components in an effort to improve predictive accuracy and to better reflect relationships between economic variables. Namely, I estimated the specifications including (1) lags of interest rate and first difference of M2 to better capture monetary policy stance; (2) GDP gap and real marginal costs for Core CPI, taken from the QPM (Quarterly Projection Model) model, to replicate the elements of a Phillips curve; (3) data on surveys, such as the index of the propensity to consume and the index of consumer sentiment to account for changes in demand. However, in most specifications I either got the wrong sign or non-significant coefficients. Only real marginal costs for Core CPI components turned out to have forecasting power. This issue should be investigated more closely in further research: new specifications, similar to the ones used by De Charsonville et al. (2017) for French data and a “thick” Phillips curve approach (both specifications with and without inflation expectations), which is regularly employed in the Eurosystem’s macroeconomic projection exercises to cross-check underlying inflation (Baumann U. et al, 2021), could be estimated.

The details on equations are represented in Table A.9, Appendix A. The magnitude of such factors as the exchange rate, nominal wages, and FAO prices is similar to that one produced in BVAR models. In addition, I may conclude that the exchange rate pass-through in the short run is smaller, and specific supply factors for each group of the RFPI are significant. The whole system of forecasting of CPI components is shown in Figure 5.

Forecasts of components are further aggregated to obtain forecasts of core and raw food indices. It is worth mentioning that State Statistic Office uses a complex system of dynamic weights, which is replicated by the NBU during the forecasting process. However, to simplify the calculations, yearly average weights are used in this paper.

⁷ See Table A.2, A.3 Appendix A with the results of data stationarity tests for levels and differences, and also Table A.9 Appendix A with the results of an Engle-Granger cointegration test for equations in levels.

4. FORECASTING PERFORMANCE

In this section I test the forecasting performance of the models. First, I describe what measures were used, and explain how the period of forecast evaluation exercise was chosen. Second, I look at forecasting performance of the models for the RFPI and its components, and then for Core CPI and its components. Finally, I analyze the forecast bias and address the issue of the quality of CPI forecasts during the COVID-19 pandemic.

4.1. Measures of Forecast Evaluation

The analysis is predominantly based on the RMSE (formula 16) indicator, as it is considered to be quite a widespread measure of a forecast’s precision. The AR model serves as a benchmark. RMSE values are shown relative to those of an AR1 model in order to facilitate the comparison (formula 17). Thus, for the given model, a value of RMSE below unity means better than the AR1 model’s precision.

Additionally, I compute a Theil index (formula 18), which also provides a measure of the distance of the true from the forecasted values. A Theil index always lies between 0 and 1, thus it makes the comparison of forecast evaluation for different components easier. For example, RMSE would usually be higher for the RFPI rather than core components because of the high volatility of raw food prices. Applying the Theil index, I can compare forecast accuracy of different indices using the same scale between 0 and 1: the closer the Theil index is to 1, the worse the forecasting accuracy.

I also analyze the forecasting bias, which is measured as the average forecast error at a certain horizon (formula 19). In turn, the forecast error is calculated as the difference between the actual value and the forecasted one. A non-zero bias indicates a possible persistent difference between the forecasts and the observed values. The formulas for the accuracy measures are the following:

$$RMSE_{j,m} = \sqrt{\sum_{t=T}^{T+h-1} (\hat{Y}_{t+j,m} - Y_{t+j})^2 / h} \quad (16)$$

$$RMSE_{j,m}^{rel} = RMSE_{j,m} / RMSE_{j,AR} \quad (17)$$

$$Theil_{j,m} = \frac{\sqrt{\sum_{t=T}^{T+h-1} (\hat{Y}_{t+j,m} - Y_{t+j})^2 / h}}{\sqrt{\sum_{t=T}^{T+h-1} \hat{Y}_{t+j,m}^2 / h} + \sqrt{\sum_{t=T}^{T+h-1} Y_{t+j}^2 / h}} \quad (18)$$

$$FBias_{j,m} = \sum_{t=T}^{T+h-1} (\hat{Y}_{t+j,m} - Y_{t+j}) / h \quad (19)$$

where $RMSE_{j,m}$, $RMSE_{j,m}^{rel}$, $Theil_{j,m}$, $FBias_{j,m}$ are consequently RMSE, RMSE relative to AR, Theil index and forecast bias of the forecast of model m , forecast horizon j . The forecast sample of length h is the following $T, T + 1 \dots T + h - 1$, $\hat{Y}_{t+j,m}$ is the forecast of model m started at time t for forecast horizon j , and Y_{t+j} is the actual value.

RMSE, the Theil index and the forecast bias are calculated for forecasts of different models as well as for combined forecasts. Equal weights are used to combine the forecasts of the following models: AR⁸, VAR, FAVAR, ECM and BVAR for raw food components, and AR, VAR, FAVAR, ECM, 4BVAR and CARMA for core inflation components.

4.2. Evaluation of the RFPI Forecasts

The forecasting evaluation exercise uses monthly data for the period of 2016m9–2021m12 for the RFPI, and 2018m03–2021m12 for Core CPI as for these periods official forecasts of the components are available and can be compared with model forecasts. It should be noted that I am interested in forecasts made in particular months, namely months when the official inflation forecast of the NBU is released and published in the Inflation Report.⁹ Assumptions are available for these particular months, which serve as exogenous variables for ECM and BVAR models. These assumptions are the same for both the other satellite models and the QPM model, which makes the short-term forecast of CPI components consistent with the predictions of other macroeconomic indicators produced by the NBU.

Table 1 shows the best performing models for each horizon and for each component of the RFPI. It can be seen

Table 1. Best Models for the RFPI and its Components (according to RMSE)

	Forecast Horizon					
	1 m	2 m	3 m	4 m	5 m	6 m
RFPI	IR	IR	CMB	CMB	AR	VAR
Cereals	IR	IR	VAR	AR	AR	VAR
Meat	BVAR	FAVAR	VAR	FAVAR	CMB	CMB
Milk	BVAR	BVAR	ECM	ECM	CMB	CMB
Eggs	IR	ECM	CMB	CMB	AR	BVAR
Vegs	BVAR	BVAR	ECM	BVAR	BVAR	CMB
Fruits	BVAR	AR	VAR	ECM	ECM	BVAR
Sugar	VAR	ECM	ECM	ECM	VAR	AR

⁸ Further in the text, for simplicity, forecasts of the different models can be identified by the following abbreviations: AR- autoregressive model, VAR-combination of bivariate VARs, FAVAR- FAVAR model, ECM – ECM model, BVAR- BVAR model for the RFPI, 3BVAR and 4BVAR are BVAR models for core CPI with three and four components, CARMA- set of ARMA models, IR- official forecasts of the NBU, CMB-combined forecast of different models using equal weights.

⁹ The Inflation Report reflects the opinion of the NBU as to the current and future economic state of Ukraine, with a focus on inflationary developments, which form the basis of monetary policy decision-making. The Inflation Report is published quarterly in accordance with the forecast periodicity.

that for most of the RFPI components, the best performing individual model differs, and the AR benchmark model is beaten in the majority of cases.

BVAR models show good forecasting performance for different components of the RFPI, especially at the beginning of the forecast horizon. That is consistent with the results of other studies that found that BVAR models with Litterman’s prior outperform alternative models such as univariate time series models and VAR models (Akdogan et al. (2012), Bloor (2009) and Hasanovic (2020)).

Table 2. RMSE Relative to AR RMSE for the RFPI

	Forecast Horizon					
	1 m	2 m	3 m	4 m	5 m	6 m
FAVAR	1.006	1.031	1.008	0.992	1.001	1.000
VAR	1.001	1.020	0.996	0.993	1.004	0.998
ECM	1.030	1.000	1.021	0.992	1.129	1.007
BVAR	0.943	1.104	0.990	1.021	1.073	1.008
CMB	0.980	0.986	0.971	0.988	1.020	0.999
IR	0.544	0.923	1.087	1.052	1.097	1.111

Compared to other methods, the ECM model forecasts some of the RFPI components relatively well for horizons from two to five months. This may reflect a link with the long-run level of prices.

Official forecasts of the NBU published in the Inflation report (named IR), appear to be the best for “cereals”, “eggs” and the RFPI for the horizon of the first month. The high forecasting accuracy of IR for the first month confirms the high precision and usefulness of nowcasting, and the importance of the incorporation of expert judgments for some components.

Combined forecasts are the best pick in around 21% of total cases: for the sixth and the fifth months of “meat” and “milk”, the sixth month of “vegetables” and also for the third and the fourth months of “eggs”. However, if we look at Table 2, presenting relative RMSE figures for the RFPI, it can be seen that even though combined forecasts are the best only for the third and the fourth months, they can beat the AR benchmark more frequently than other types of models. Accuracy might be improved even further if a more sophisticated system of weights is used. For example, Akdogan et al. (2012) uses inverse RMSE weights, whereas in Timmerman (2006) other generalizations are discussed.

The formula for the inverse RMSE weights is the following:

$$w_{jm} = \frac{RMSE_{j,m}^{-1}}{\sum_{m=1}^M RMSE_{j,m}^{-1}} \quad (20)$$

Where $m = 1..M$ is m-th type of model, $j = 1..h$ is the forecast horizon, and $RMSE_{j,m}$ is RMSE for m-th model for the j-th horizon.

The plots with RMSE and the Theil index for the RFPI components can be found in Figures B.4, B.6, Appendix B. As the scale of the Theil index is similar to each component,

comparisons of accuracy between the groups can be made. According to the Theil index, the forecasts for “milk”, “meat”, “fruits” and “vegetables” prices seem to be more accurate than the forecasts of the other components. Forecasts of “sugar” from the second to the sixth month have the lowest precision. In general, the forecasts of the RFPI index are of decent accuracy. This may be due to the high accuracy of the forecasts of its main components. Another reason may be the fact that the error forecasts of different components are canceled out while aggregating the forecasts of components into RFPI forecasts. I further analyze forecast bias to check this hypothesis.

Plots of forecast bias can be found in Figure B.8, Appendix B. Indeed, for various components and models forecast bias is either negative or positive and has different patterns, which may support the hypothesis on the canceling out of errors while aggregating the RFPI forecasts. The forecast bias of the RFPI for most of the models is the smallest: it is slightly positive for the first three months, and then becomes slightly negative. Also, the forecast bias of more volatile components like “eggs”, “vegetables” and “fruits” is larger. The bias patterns of various models for “meat”, “milk” and the RFPI are different, this fact may lead to gains in forecast accuracy for combined forecasts of these prices.

Finally, I would like to discuss the models’ accuracy during the COVID-19 pandemic, which covers the period from 2020m3 to 2021m12. As shown in Figure 6, the percentages of models that have the best accuracy for different horizons and components for the whole sample of forecasting exercise differ from those in COVID-19 pandemic times. The decrease in the percentage of combined forecasts by 17 ppt may be attributed to the above-mentioned fact that an equal weighting scheme is not optimal for combined forecasts. The increase in the percentage of multivariate models (FAVAR and VAR altogether) by 8 ppt shows the effectiveness of using models with a broad information set in times of crises and other extraordinary events. The better forecasting performance of the ECM model may have the same origin: the ECM model’s equations contain a lot of factors individual to each group, namely, supply side factors (such as harvest and production) as well as a variety of international prices.

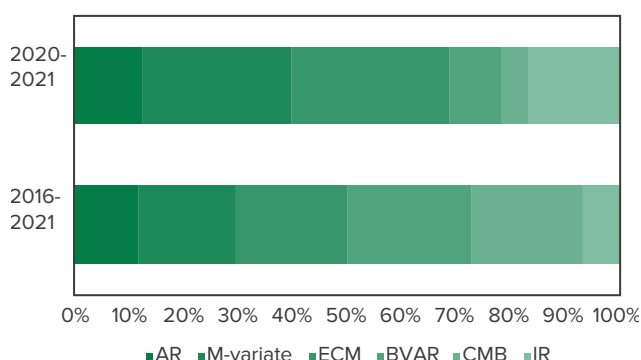


Figure 6. Percentages of Types of Models with the Best Forecasting Performance for Different Forecast Horizons and Components¹⁰, RFPI

¹⁰ The percentages for the whole sample of forecasting exercise (2016-2021) correspond to the frequency of the type of model represented in the Table 1. The similar was done for the part of forecasting exercise sample (2020-2021) to access the models’ performance during COVID-19 pandemic. M-Variate includes FAVAR and VAR models.

Table 3. Best Models for Core CPI and Its Components (according to RMSE)

	Forecast Horizon					
	1 m	2 m	3 m	4 m	5 m	6 m
Core CPI	CMB	CMB	CMB	CMB	CMB	CMB
Processed food	IR	CMB	CMB	CMB	IR	3BVAR
Services	AR	CMB	CMB	CARMA	CMB	CMB
Cloth and shoes	CARMA	ECM	CARMA	CMB	CMB	CARMA
Others	IR	CMB	4BVAR	4BVAR	4BVAR	CMB

4.3. The Evaluation of Core CPI forecasts

Contrary to the RFPI components, for core CPI and its components the models that have the best precision are not so diverse: combined forecasts are the best for core CPI and partly for other components, CARMA is the best partly for “services” and for “clothes and shoes”, while BVAR is the best partly for “processed food” and for “others” (see Table 3).

For the “clothes and shoes” group CARMA turned out to be the best model for almost the whole forecast horizon. The good performance of the CARMA model means that the precision of a univariate model is higher than that of multivariate ones. The reason for this is likely due to the statistical properties of both of these groups (prices for “clothes and shoes” follow the ARMA process well enough and are less volatile than food prices) and the scarcity of the multivariate models’ information dataset for the “clothes and shoes” group. A similar conclusion for a slightly richer information dataset was made by Aastveit et al. (2011) regarding inflation forecasting in Norway. Using new explanatory variables for these groups would probably improve the forecasts of multivariate models.

The combined forecasts of core CPI turned out to be the most precise, outperforming other models’ forecasts significantly (see Table 4), and confirming the conclusions of Kapetanios et al. (2007) and Bjornland et al. (2008) regarding the superiority of combined forecasts. Such large gains in precision were achieved because for some models the bias is positive, while for other models it is negative (see

Figure B.9 in Appendix B). Thus, the combination of models’ forecasts led to a more precise and unbiased outcome.

For all of the core CPI components, except for the “clothes and shoes” component, the sign of the bias varies across the models. Forecasts for the “clothes and shoes” component show a consistent positive bias for all types of models. This may be partly explained by changes in the methodology. In 2014, the SSSU began including sales prices, thus decreasing the overall level of prices.

According to the Theil index (see Figure B.7 in Appendix B), forecasts of core CPI components are more precise than those of the RFPI components, “clothes and shoes” forecasts being the most accurate. However, for the “others” group the forecasts are the least accurate since it is very hard for this group to find appropriate indicators, explaining the price dynamic.

For Core CPI components, the shift in best types of models during COVID-19 pandemic times is more profound: there is a slump in the percentage of combined forecasts (from 57 to 7%) and increase in the percentage of IR forecasts (from 10% to 30%). The increase in precision of IR forecasts shows that in crisis times expert judgments may improve forecasts significantly. Similarly to the RFPI components, multivariate models such as FAVAR and VAR appeared to be highly precise in pandemic times: their percentage reached 27%.

The worsening in the performance of the models using exogenous variables (the percentage of BVAR and ECM

Table 4. RMSE Relative to AR RMSE for Core CPI

	Forecast Horizon					
	1 m	2 m	3 m	4 m	5 m	6 m
CARMA	0.706	1.100	1.077	0.902	1.120	1.184
FAVAR	0.877	1.055	1.011	0.964	0.965	0.976
VAR	0.878	1.006	1.017	1.008	1.017	1.000
ECM	1.042	1.815	1.768	1.414	1.622	1.473
4BVAR	0.914	1.333	1.118	1.011	1.227	1.134
3BVAR	0.982	1.438	1.498	1.261	1.412	1.260
CMB	0.628	0.903	0.942	0.830	0.909	0.920
IR	0.875	1.218	1.442	1.385	1.230	1.187

altogether decreased by 10ppt) may be due to the fact that the assumptions on the exogenous variables used in the models remarkably differed from the actual realizations of the data, thus worsening the forecasting ability of the models with exogenous variables.

To verify this, I calculated forecasts for ECM and BVAR models using actual realizations of the data instead of assumptions for exogenous variables. The RMSE of the models can be seen in Figure B.10, Appendix B. RMSEs of the models using actual data are lower than that ones' using assumptions, the difference between the RMSEs being wider for Core CPI. Thus, there is evidence that the difference between actual data and assumptions may further increase the forecasting error.

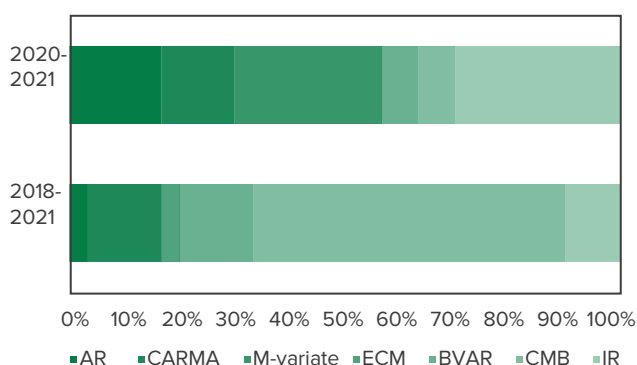


Figure 7. Percentages of Types of Models with the Best Forecasting Performance for Different Forecast Horizons and Components, Core CPI

4.3.1. Comparison of the QPM Forecasts and Combined Forecasts of the Suite of Models

The QPM¹¹ is the core model of the FPAS system at the NBU. At its core it has a set of theory-based relationships that capture the key part of the transmission mechanism. It provides the organizational framework for macroeconomic forecasting and story-telling, as well as having to be able to forecast the main economic indicators. Karam et al (2006) argue that in many central banks it is recognized that the model is much less accurate than experts at forecasting the first one or two quarters. That is why, to improve the forecasting qualities of the core model, the final forecast can be a hybrid of the QPM and short-term forecasting models, i.e the QPM forecast could include short-term tunes coming from satellite models.

Table 5. RMSE Relative to AR RMSE for q-o-q Core CPI

	Forecast Horizon	
	1 q	2 q
CMB	0.79	0.84
QPM	1.11	0.86

The best forecasts for core inflation i.e., combined forecasts, were transformed to quarterly frequency in order to compare the forecasting accuracy of the short-term

forecasting system with that of QPM. CMB outperforms QPM in both the first and second quarters. However, in the first quarter the difference is more profound (the RMSE relative to AR can be found in Table 5).

Given the fact that the core inflation forecasts of the short-term forecasting models for the first and second quarters are more accurate than QPM's, we can incorporate the results of the suit of models into the QPM model in the form of short-term tunes. This will allow us to receive more precise short-term QPM forecasts.

5. CONCLUSIONS

This study reviews the suite of models used by the NBU for short term CPI forecasting and tests the forecasting properties of the employed models (univariate models (AR, ARMA), vector autoregressive (VAR) models, factor augmented VAR (FAVAR) models, Bayesian VAR (BVAR) models, and error correction models (ECM)), while the AR model serves as a benchmark. The forecasting evaluation exercises use monthly data for the period of 2016–2021. The findings of the paper suggest the following:

First, for almost all components of CPI there are models that outperform the benchmark AR models. BVAR models show good forecasting performance for different components of core CPI and the RFPI. This result is consistent with the conclusions of other studies arguing that BVAR models with Litterman's prior outperform alternative models, such as univariate time series models and VAR models. However, for the groups "services" and "clothes and shoes", the ARMA model forecasts turned out to be the most accurate. Similar results were observed in a Bank of Norway paper that showed that a rich data set added little extra value to multivariate models' performance.

Second, combined forecasts obtained by averaging models' forecasts produce acceptable and robust results, i.e. for core inflation the combined forecasts are the most precise ones, while for the raw food price index they beat the AR benchmark more frequently than other types of models. Thus, these findings confirm the conclusions of Kapetanios et al. (2007) and Bjornland et al. (2008) regarding the superiority of combined forecasts in comparison to individual model forecasts.

Third, the high forecasting accuracy of the official forecasts for the first month proves the precision and usefulness of nowcasting and the importance of incorporating expert judgments for some CPI components. In addition, the combined forecasts of core inflation for the first two quarters are more accurate than the forecasts produced by QPM. Hence, it looks promising to incorporate the results of a suite of models in the form of short-term tunes into the QPM model in order to receive more precise short-term QPM forecasts.

Fourth, the analysis of forecasting performance of the models during COVID-19 pandemic compared to the performance during the whole forecasting sample showed that models with a broad information set are more effective in times of crises or other extraordinary events. However, expert judgments also may improve forecasts significantly.

Even though this paper analyzes forecasts of inflation up to the end of 2021, it is worth briefly mentioning the influence of the russian invasion of Ukraine which began

¹¹ QPM is a semi-structural, forward-looking New-Keynesian model of a small open economy. It is a main element of the FPAS at the NBU. Detailed information regarding the QPM model can be found in Grui and Vdovychenko (2019).

on 24 February 2022 and highlight key challenges for forecasting CPI components in wartime. After the shock of the first weeks of war, economic activity began reviving in the relatively calm and liberated regions. In the first quarter of 2022, real GDP, decreased by 15.1% yoy. The slump in the second quarter was even deeper (-37.2%) due to large numbers of damaged and destroyed factories, enterprises and infrastructure. Additionally, there is a negative impact from the outflow of the labor force as well. In June 2022, consumer inflation accelerated to 21.5% yoy. The faster inflation was caused by both global trends (high energy prices) and internal factors (disrupted supply chains, higher production costs, and stronger household demand for some goods and services on the back of insufficient supply). Additionally, price pressure is uneven across the country's regions: the highest price hikes are in the temporarily occupied regions and in cities with active hostilities.

Measures taken by the government and the NBU partially offset the inflationary pressure caused by Russia's full-scale invasion. The NBU was forced to fix the exchange rate and impose a number of administrative restrictions, including ones on FX transactions and capital movements, so as to maintain price and financial stability and to control inflation expectations. After that, on June 1, the NBU Board decided to raise the key policy rate to 25%. This is intended to spur investors' interest in hryvnia assets, while also easing pressures on international reserves and reining in inflation.

Thus, forecasting economic indicators in Ukraine in the near future will be very challenging, because of:

- Difficulties with data. The State Statistic Services of Ukraine announced that it will cease publishing the most of its official data during the war. The data on the CPI components, exchange rates, and international prices are still available but other information, such as that on economic output and labor statistics, has become

heavily restricted or even unobservable and, therefore, researchers are forced to make numerous assumptions while modelling. It is not also clear how the statistics are being gathered in the occupied regions, and how the shift in consumption patterns had affected the data. In such circumstances limited data availability can cause some selection and estimation biases that might ultimately result in difficulty with forecasting. Soft data with a high frequency might be of benefit in this case.

- Structural changes. From the very beginning of the active phase of the war, drastic structural changes may have altered the statistical properties of data and the relationships between macroeconomic indicators. In these circumstances, expert judgements could be of great help (as during the COVID-19 pandemic). To learn of the experiences of other countries affected by wars, military conflicts, or natural disasters may also be beneficial for CPI forecasting in wartime.

Based on the results above, there are several ways to improve the existing suite of models and make its forecasts more accurate and better grounded:

- The BVAR model for Core CPI components could benefit from resolving the issue with the endogeneity of the existing indicators.

- The results from surveys, information obtained from non-conventional data sources like Google trends, etc. can enrich the dataset for FAVARs and bivariate VARs.

- New specifications, similar to ones used by De Charonville et al. (2017) for French data and the "thick" Phillips curve approach (both specifications with and without inflation expectations), which is regularly employed in the Eurosystem's macroeconomic projection exercises (Baumann U. et al, 2021), could be estimated.¹²

- More sophisticated weighting schemes could be applied to combined forecasts in order to increase their precision.

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¹² We thank an anonymous referee for this suggestion.

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APPENDIX A. TABLES

Table A.1. Methods and Techniques Used in CBs for Short-Term Forecasting

Authors	Bank	Object	Models	Models with best accuracy	Estimation period and reestimation	Forecast period	Density or point forecast	Combination	Judgements
Aastveit et al. (2011)	BoN	CPI excl taxes and energy	AR models for main CPI components, bivariate VAR, VAR, BVAR, VECM, Factor models	bivariate VARs	1982Q4 or 1993Q1, depending on the approach	1-2Q	density	yes	yes
Akdogan et al. (2012)	CBRT	CPI excl unprocessed food and tobacco, no disaggregation	Univariate models, Nonlinear models, Phillips curve motivated time varying parameter model, VAR, BVAR, Dynamic factor models	BVAR	2003-2011	1-2Q	point	yes	yes
Alvarez, Sanchez (2017)	BoS	CPI, disaggregated 120 items, CPI excluding food and energy	Univariate models, Transfer function models, Phillips curve motivated model	Transfer function models	since 2012	1-3Q	point	no info	yes
Bloor (2009)	RBNZ	CPI, GDP (both short and medium term forecasting)	1. VARs (both classical and bayesian VARs, VECM) 2. Leading indicators models (bivariate VARs, bridge equations, AR) 3. Factor models	Combined forecast of leading indicators models	forecast exercise sample 2000-2008	1-8Q	not clear	not clear*	yes
De Charsonville et al. (2017)	BoF	HICP, 5 items and administered prices, 21 components for 3M	ARIMA, ECM	ECM	1996Q1/2007Q3**-2014Q4	1-12Q 1-12M	point	no	yes
Giannone et al. (2010)	ECB	HICP, 5 items, PPI	BVAR	BVAR	since 1991	1-18 M	density	no info	yes
Mazur (2022)	NBP	CPI, disaggregated 42 components	S-ARIMA, Dynamic factor model, Leading indicator, BAR, BVAR	no info	no info	1-12M	density	yes	yes

Table A.1 (continued). Methods and Techniques Used in CBs for Short-Term Forecasting

Authors	Bank	Object	Models	Models with best accuracy	Estimation period and reestimation	Forecast period	Density or point forecast	Combination	Judgements
Hasanovic (2020)	CBBH	CPI	ARMA,VAR, BVAR	BVAR	2007-2017	1-12M	point	no info	no info
Rummel (2015)	BoE	CPI, disaggregated 31 items	Naive sample average, ARMA, VARMA, FAVAR	no info	no info	1-6M	density	yes	yes

* As for 2009, RBNZ was considering the benefits of model averaging versus forecasts from individual forecasts, and the possible use of density forecast instead of point forecasts.

** The size of the sample varies for each component.

Table A.2. Time Series Used for Forecasting

Name	Description	Source	Beginning of Sample/frequency	Source of data forecasts (for exogenous)	Seasonality test	Stationarity test		
						ADF Prob (level)	ADF Prob (1st diff)	ADF Prob (yoy diff)
	IMF prices of							
IMF_P_WHT	wheat	IMF	2004/m	IMF OUTLOOK	NP	0.27	0.00	0.00
IMF_P_BRL	barley				P	0.50	0.00	0.00
IMF_P_SOY	soybeans				NP	0.09	0.00	0.00
IMF_P_CHCK	chicken				NP	0.50	0.00	0.00
IMF_P_OIL	sunflower oil				NP	0.02	0.00	0.00
IMF_P_SGR	sugar				P	0.33	0.00	0.00
	FAO price index of							
FAO_P_F	food	FAO	2004/m	MPEAD assessments	NP	0.56	0.00	0.00
FAO_P_CRL	cereals				Probably NP	0.48	0.00	0.01
FAO_P_MT	meat				Probably NP	0.33	0.00	0.00
FAO_P_CHCK	chicken				NP	0.34	0.00	0.00
FAO_P_BF	beef				NP	0.76	0.00	0.00
FAO_P_PRK	pork				P	0.10	0.00	0.00
FAO_P_DAI	dairy products			REUTERS	NP	0.19	0.00	0.00
FAO_P_SGR	sugar				NP	0.29	0.00	0.00
	WB prices of							
WB_P_CRL	cereals	WB	2004/m	MPEAD assessments	P	0.46	0.00	0.03
WB_P_FUEL	energy				NP	0.16	0.00	0.00
WB_P_OIL	sunflower oil			WB OUTLOOK	NP	0.14	0.00	0.00
WB_P_FRT	fertilizers				NP	0.51	0.00	0.00
WB_P_BN	bananas				NP	0.78	0.00	0.00
WB_P_ORN	oranges				NP	0.00	0.00	0.00
WB_P_SGR	sugar				NP	0.29	0.00	0.00

Table A.2 (continued). Time Series Used for Forecasting

Name	Description	Source	Beginning of Sample/ frequency	Source of data forecasts (for exogenous)	Seasonality test	Stationarity test		
						ADF Prob (level)	ADF Prob (1st diff)	ADF Prob (yoy diff)
	Other indicators							
EC_P_EGG	Eggs prices in EU	EU com- mission	2004/m	MPEAD assessments	P	0.05	0.00	0.00
DISEL_P_UAH	Diesel prices in Ukraine	NBU/ web- scraping	2005/m		NP	0.65	0.00	0.00
ER_EU_USD	Euro/USD exchange rate	Reuters	2001/m		NP	0.12	0.00	0.00
ER_M	UAH/USD exchange rate	NBU	2001/m		NP	0.98	0.00	0.00
NWAGE	Nominal average wage	SSSU	2005/m		P	1.00	0.00	0.00
MINWAGE	Nominal minimum wage	SSSU	2005/m		NP	1.00	0.00	0.15
RMC_C	Real monetary costs for Core CPI	NBU (QPM)	2004/q					
PPI_EUD	Non-durable consum- er goods (EU28 PPI)	OECD	2010/m		P	0.52	0.00	0.01
AGR	Average sale prices for agricultural prod- ucts	SSSU	2005/m		Probably NP	0.79	0.00	0.00
	Production of							
PR_EGG	eggs		2001/m	MPEAD assessments	P	0.84	0.18	0.80
PR_MT	meat				P	1.00	0.00	0.00
PR_MILK	milk				P	0.37	0.00	0.00
	Harvest of							
CRL_H	cereals	SSSU	2001/y	MPEAD assessments				
FRT_H	fruits							
POTATO_H	potato							
SGR_H	sugar							
VGT_H	vegetables							
OIL_H	sunflower seeds							

Note: Results of the seasonality test for the Combined test, indicating whether there is the presence of identifiable seasonality. P stands for present, NP – not present. It is recommended that a series is adjusted in the cases of P and Probably NP, and not adjusted in the case of NP.

Stationarity test shows the p-values of ADF test for levels, 1st differences and yoy changes. Quarter and year frequency data converted into monthly frequency using cubic spline.

Table A.3. Components of the CPI and the PPI

Name	Description	Source	Beginning of Sample/ frequency	Seasonality test	Stationarity test		
					ADF Prob (level)	ADF Prob (1st diff)	ADF Prob (yoy diff)
	CPI						
CPI_F	RFPI	SSSU	2004/m	P	0.86	0.00	0.07
CPI_MT	meat			P	0.91	0.00	0.00
CPI_MLK	milk			P	0.88	0.00	0.02
CPI_EGGs	eggs			P	0.73	0.00	0.00
CPI_FRT	fruits			P	0.74	0.00	0.01
CPI_VGT	vegetables			P	0.13	0.00	0.00
CPI_SGR	sugar			NP	0.88	0.00	0.00
CPI_CRL	cereals			NP	0.91	0.00	0.00
CPI_OIL	Sunflower oil, CPI			NP	0.86	0.00	0.00
CPI_FUEL	Fuel component of CPI		2004/m	NP	0.53	0.00	0.02
CPI_C	Core CPI		2012/m	NP	0.74	0.01	0.05
CPI_FC	processed food			NP	0.79	0.00	0.03
CPI_SRV	services			NP	0.98	0.01	0.03
CPI_CLSH	clothes and shoes			P	0.52	0.02	0.64
CPI_OTHR	others			NP	0.50	0.01	0.35
CPI_FOTHR	processed food and others			NP	0.63	0.01	0.08
	PPI						
PPI_F	processed food		2012/m	NP	0.79	0.00	0.00
PPI_MT	meat			NP	0.53	0.00	0.01
PPI_MLK	milk			NP	0.68	0.00	0.00
PPI_CRL	cereals			NP	0.88	0.00	0.01
PPP_SGR	sugar			Probably NP	0.84	0.00	0.00
PPI_CLSH	clothes and shoes			NP	0.96	0.00	0.03
PPI_COMP	computers			NP	0.57	0.00	0.58
PPI_AUTO	cars			NP	1.00	0.00	0.17

Note: Results of the seasonality test for the Combined test, indicating whether there is the presence of identifiable seasonality. P stands for present, NP – not present. It is recommended that a series is adjusted in the cases of P and Probably NP, and not adjusted in the case of NP.

Stationarity test shows the p-values of ADF test for levels, 1st differences and yoy changes.

Table A.4. AR Models for the RFPI and Core Inflation

Forecasted Variable	Lags	AR coefficient	Sample	S.E.
CPI_MT	1	0.65	2005m3-2021m12	1.09
CPI_MLK	2	0.69	2005m4-2021m12	0.86
CPI_EGGs	2	-0.11	2005m4-2021m12	8.76
CPI_FRT	1	0.36	2005m3-2021m12	3.93
CPI_VGT	1	0.31	2005m3-2021m12	6.39
CPI_SGR	1	0.38	2005m3-2021m12	5.21
CPI_CRL	4	0.50	2005m6-2021m12	3.10
CPI_FC	2	0.67	2014m4-2021m12	0.26
CPI_SRV	1	0.40	2014m3-2021m12	0.31
CPI_CLSH	1	0.29	2014m3-2021m12	0.61
CPI_OTHR	1	0.52	2014m3-2021m12	0.33

Table A.5. Data Sets for Bivariate VARs and FAVAR Models for Each Forecasted Variable

Forecasted variable	Data set
CPI_MT	fao_p_mt, fao_p_chck, fao_p_prk, fao_p_bf, fao_p_crl, imf_p_wht, imf_p_brl, imf_p_soy, imf_p_chck, imf_p_oil, wb_p_crl, wb_p_fuel_l
CPI_MLK	fao_p_dai, fao_p_crl, imf_p_wht, imf_p_brl, imf_p_soy, imf_p_oil, wb_p_crl, wb_p_fuel"
CPI_EGGs	fao_p_crl, imf_p_chck, imf_p_wht, imf_p_brl, imf_p_soy, imf_p_oil, wb_p_chck, wb_p_crl, wb_p_fuel, ec_p_egg
CPI_FRT	fao_p_f, imf_p_f, imf_p_bn, imf_p_orn, wb_p_f, wb_p_orn, wb_p_bn, wb_p_fuel, wb_p_frt
CPI_VGT	fao_p_f, imf_p_f, wb_p_f, wb_p_fuel, wb_p_frt
CPI_SGR	fao_p_sgr, imf_p_sgr, wb_p_sgr, wb_p_fuel, wb_p_frt
CPI_CRL	fao_p_crl, imf_p_wht, imf_p_brl, wb_p_crl, wb_p_fuel, wb_p_frt
CPI_FC	agr, cpi_f, cpi_fuel, disel_p_uah, er_eu_usd, er_m, fao_p_f, imf_p_f, minwage, nwage, ppi_eund, ppi_f, rmc_c, wb_p_f
CPI_SRV	cpi_fc, er_eu_usd, er_m, minwage, nwage, rmc_c
CPI_CLSH	er_eu_usd, er_m, minwage, nwage, ppi_eud, rmc_c
CPI_OTHR	er_eu_usd, er_m, minwage, nwage, ppi_eud, rmc_c

Table A.6. Lag Length Criteria for BVAR Models

	LR	FPE	AIC	SC	HQ
BVAR_RFPI	4	2	2	1	1
BVAR_3CORE	2	2	2	1	1
BVAR_4CORE	2	2	2	1	1

Note: numbers in the Table A.6 indicate lag order selected by the criterion:

LR: sequential modified LR test statistic (each test at 5% level)

FPE: Final prediction error

AIC: Akaike information criterion

SC: Schwarz information criterion

HQ: Hannan-Quinn information criterion

Table A.7. Grid Search

	Minimum value	Maximum value	Step size
Autoregressive coefficient	0.20	1.00	0.10
Overall tightness (λ_1)	0.05	0.20	0.01
Cross-variable weighting (λ_2)	0.10	1.00	0.10
Lag decay (λ_3)	0.10	2.00	0.20
Exogenous variable tightness (λ_4)	100	1000	100

Table A.8. BVAR Model Specifications

Endogenous variables	Exogenous variables	lags	Sample	Hyper parameters	total number of iterations:	burn-in iterations:
7 RFPI components (CPI_MT, CPI_MLK, CPI_EGGs, CPI_FRT, CPI_VGT, CPI_SGR, CPI_CRL)	ER_M(-1), FAO_P_F(-1)	2	2005 m1-2021m12	Mu1: 0.5, λ_1 : 0.05, λ_2 : 1, λ_3 : 1, λ_4 : 100	10000	5000
3 core CPI components (CPI_FOTHR, CPI_SRV, CPI_CLSH)	NWAGE, ER_M(-1)	2	2012m1-2021m12	Mu1: 0.5, λ_1 : 0.05, λ_2 : 1, λ_3 : 1, λ_4 : 100	10000	5000
4 core CPI components (CPI_FC, CPI_SRV, CPI_CLSH, CPI_OTHR)	NWAGE, ER_M(-1)	2	2012m1-2021m12	Mu1: 0.4, L1: 0.11, L2: 1, L3: 1, L4: 100	10000	5000

Table A.9. Equations for Components of the RFPI and Core CPI

eq name	SE	Coin- tegra- tion test	AR(1)	COI	factors	factors	factors	factors	factors
crl	2.60	0.07	D(CPI_ CRL_L(-1)) 0.5	CRL_ COI2(-1) -0.06	D(ER_M_L(-1)) 0.40	D(FAO_P_CRL_L) 0.10	D(WB_ P_FRT_L(-1)) 0.10	D(CRL_H_ LQS(-5)) -0.20	
mt	0.90	0.06	D(CPI_ MT_L(-1)) 0.60	MT_ COI2(-1) -0.05	D(ER_M_L(-1)) 0.10	D(FAO_P_MT_L(-1)) 0.01	D(CPI_ OIL_L) 0.10	C 0.20	
mlk	0.80	0.08	D(CPI_ MLK_L(-1)) 0.60	MLK_ COI2(-1) -0.03	D(ER_M_L(-1)) 0.04	D(FAO_P_ DAI_L(-2)) 0.04	D(CPI_ OIL_L) 0.10	C 0.30	
egg	7.80	0.00	D(CPI_ EGG_L(-1)) 0.20	EGG_ COI2(-1) -0.32	@MOVAV (D(ER_M_L(-1)),3) 0.30	D(EC_P_ EGG_L(-0)) 0.20	D(CPI_ OIL_L(-2)) 0.40	D(PR_ EGG_L(-1)) -0.30	D(PR_ EGG_L(-2)) -0.40
frt	3.50	0.13	D(CPI_ FRT_L(-1)) 0.30	FRT_ COI2(-1) -0.07	D(ER_M_L(-1)) 0.30	D(DISEL_P_ UAH_L) 0.20	D(IMF_ P_BN_L(-1)) 0.10	D(FRT_H_ LQS(-2)) -0.30	
vgt	5.80	0.02	D(CPI_ VGT_L(-1)) 0.30	VGT_ COI2(-1) -0.14	D(ER_M_L(-1)) 0.20	D(VGT_H_LQS(-2)) -1.40	D(POTATO_ H_LQS) -1.00	D(FAO_ P_F_L) 0.30	@SEAS(7) 4.40
sgr	4.0	0.00	D(CPI_ SGR_L(-1)) 0.3	SGR_ COI2(-1) -0.10	D(ER_M_L(-1)) 0.3	@MOVAV(D (FAO_P_SGR_L),3) 0.2	D(DISEL_P_ UAH_L) 0.3	D(SGR_H_ LQS(-7)) -0.4	
fc	0.50	0.02	D(CPI_ FC_L(-1)) 0.60	FC_ COI2(-1) -0.05	D(ER_M_L(-1)) 0.20	D(ER_M_L(-0)) 0.03	D(CPI_F_L) 0.10		
srv	0.30	0.02	D(CPI_ SRV_L(-1)) 0.60	SRV_ COI2(-1) -0.03	@MOVAV (D(ER_M_L(-0)),2) 0.10	@MOVAV (D(NWAGE_L),5) 0.20			
clsh	0.90	0.00	D(CPI_ CLSH_L(-1)) 0.10	CLSH_ COI2(-1) -0.25	@MOVAV (D(ER_M_L(-1)),6) 0.20	D(@MOVAV (COVDUM,4)) -3.90	RMC_C(-3) 0.10		
othr	0.40	0.00	D(CPI_ OTHR_L(-1)) 0.60	OTHR_ COI2(-1) -0.02	D(ER_M_L(-1)) 0.10	D(ER_M_L(0)) 0.10	D(DISEL_P_ UAH_L) 0.00		

Note: Co-integration test shows z-statistic of the Engle-Granger Co-integration test for the long-run equation. Value less than 0.05/0.10 rejects the null hypothesis of no co-integration at a significance level of 5/10%.

APPENDIX B. FIGURES

	Mean	St. dev.	2013	2014	2015	2016	2017	2018	2019	2020	2021
CPI	13.4	14.4									
Fuel	13.7	21.6									
Food and non-alcoholic beverages	12.4	14.0									
Rice	15.8	33.4									
Bread	17.4	15.9									
Pasta	12.9	16.6									
Beef and veal	12.3	12.7									
Pork	10.4	15.1									
Poultry	12.7	15.3									
Other meats	11.8	9.0									
Fish and seafood	11.7	19.6									
Fresh whole milk	12.7	9.1									
Yoghurt	12.7	7.9									
Cheese and curd	12.0	7.2									
Eggs	16.8	34.4									
Butter	13.6	9.2									
Margarine and other vegetable fats	14.1	14.2									
Olive oil	12.6	21.8									
Other edible oils	18.0	29.8									
Fruit	14.6	29.7									
Citrus fruits	10.5	31.5									
Banana	11.1	30.2									
Apples	18.5	43.9									
Dried fruits	15.2	34.2									
Vegetables	6.6	25.3									
Cabbage	28.5	84.1									
Cucumbers, tomatoes, pepper, zucchini	-5.1	28.7									
Potatoes	9.9	40.4									
Preserved or processed vegetables	12.2	13.9									
Potatoes	19.0	40.7									
Borsch vegetables	24.7	57.8									
Sugar	17.9	28.5									
Chocolate	14.0	27.2									
Coffee, tea and cocoa	13.5	24.8									
Mineral waters, soft drinks, fruit and vegetable juices	11.1	9.4									
Alcoholic beverages	12.7	10.3									
Tobacco	22.2	10.3									
Clothing	4.5	11.7									
Other articles of clothing and clothing accessories	8.4	10.1									
Cleaning, repair and hire of clothing	13.1	6.5									
Shoes and other footwear	5.1	13.9									
Repair and hire of footwear	11.5	6.9									
HOUSING, WATER, ELECTRICITY, GAS AND OTHER FUELS	26.6	40.7									
Actual rentals for housing	7.6	4.3									
Imputed rentals for housing	2.5	3.3									
Maintenance and repair of the dwelling	11.1	11.4									
Water supply and miscellaneous services relating to the dwelling	22.3	18.2									
Electricity	22.4	26.4									
Gas	57.3	125.7									
Solid fuels	6.4	11.0									
Heat energy	26.2	33.4									
Furniture and furnishings, carpets and other floor coverings	9.3	11.8									
Household textiles	9.2	14.7									
Household appliances	8.8	15.4									
Glassware, tableware and household utensils	9.7	15.1									
Tools and equipment for house and garden	9.0	15.5									
Goods and services for routine household maintenance	9.3	16.3									
Medical products, appliances and equipment	12.9	16.2									
Out-patient services	12.4	6.4									
Hospital services	10.8	4.9									
Purchase of vehicles	13.8	26.5									
Operation of personal transport equipment	13.2	17.9									
Fuels and lubricants for personal transport equipment	13.7	21.6									
Passenger transport by railway	11.3	7.7									
Passenger transport by road	15.3	11.0									
Passenger transport by air	7.9	10.7									
Postal services	21.4	27.6									
Telephone and telefax equipment	-0.3	13.6									
Telephone and telefax services	8.3	6.6									
Audiovisual, photographic and information processing equipment	2.8	14.7									
Other recreational items and equipment, gardens and pets	11.5	18.9									
Recreational and sporting services	8.8	3.5									
Cultural services	12.6	6.5									
Newspapers, books and stationery	9.2	12.0									
Package holidays	16.3	27.7									
Pre-primary and primary education	18.9	14.7									
Secondary education	12.3	5.4									
Tertiary education	10.2	5.0									
Education not definable by level	9.6	3.6									
Restaurants, cafés and the like	10.4	6.5									
Canteens	13.4	9.3									
Accommodation services	8.0	5.2									
Hairdressing salons and personal grooming establishments	10.7	4.0									
Other appliances, articles and products for personal care	11.2	17.6									
Personal effects n.e.c.	8.0	14.4									
Insurance	10.5	13.3									
Financial services n.e.c.	8.6	7.2									
Other services n.e.c.	10.1	5.7									

Figure B.1. Heat Map



Figure B.2. Consumption Balances

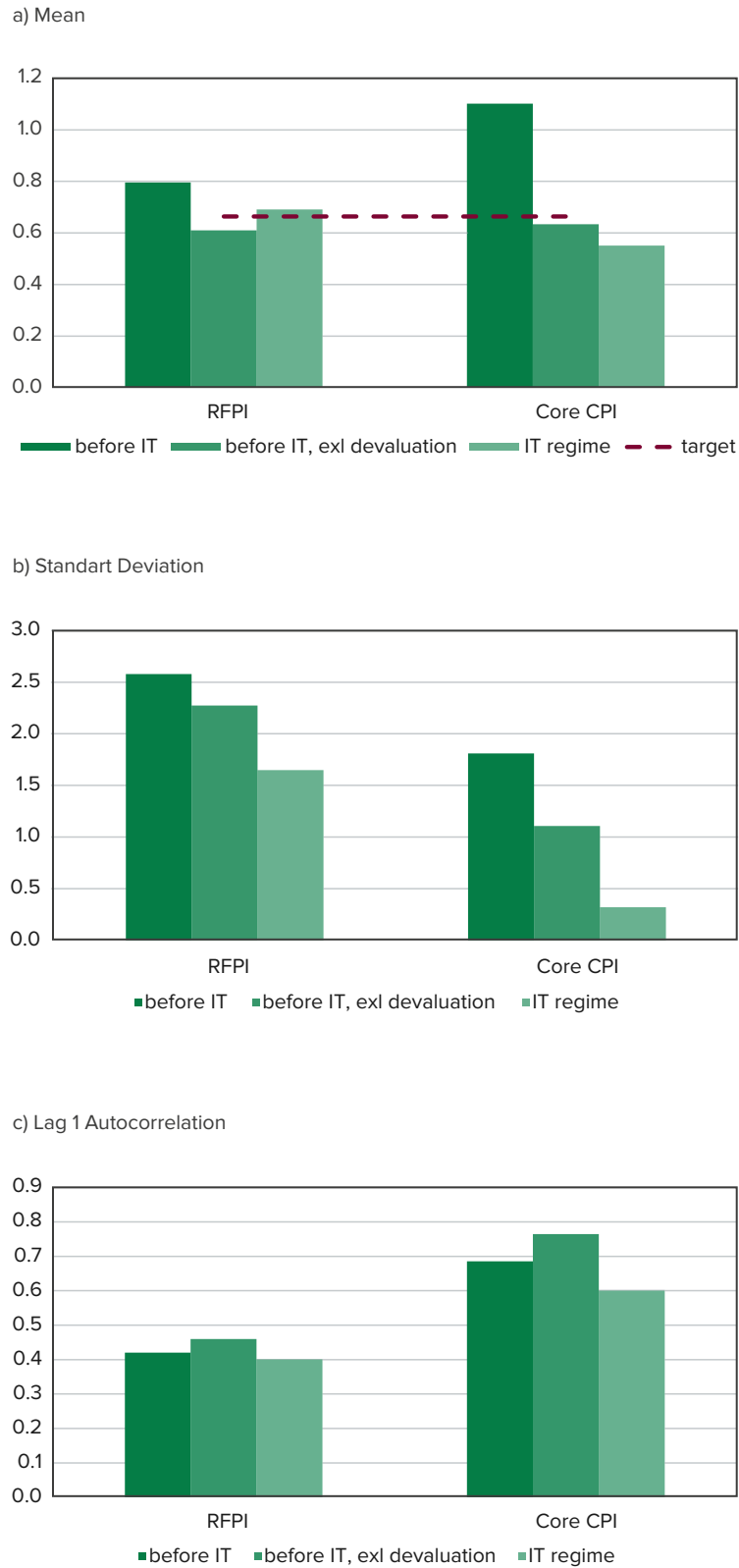


Figure B.3. Statistical Properties of the Data on RFPI and CPI for pre-IT- and IT Regime Data Samples

Note: Data samples for RFPI and Core CPI start in 2005m1 and 2012m1 respectively.

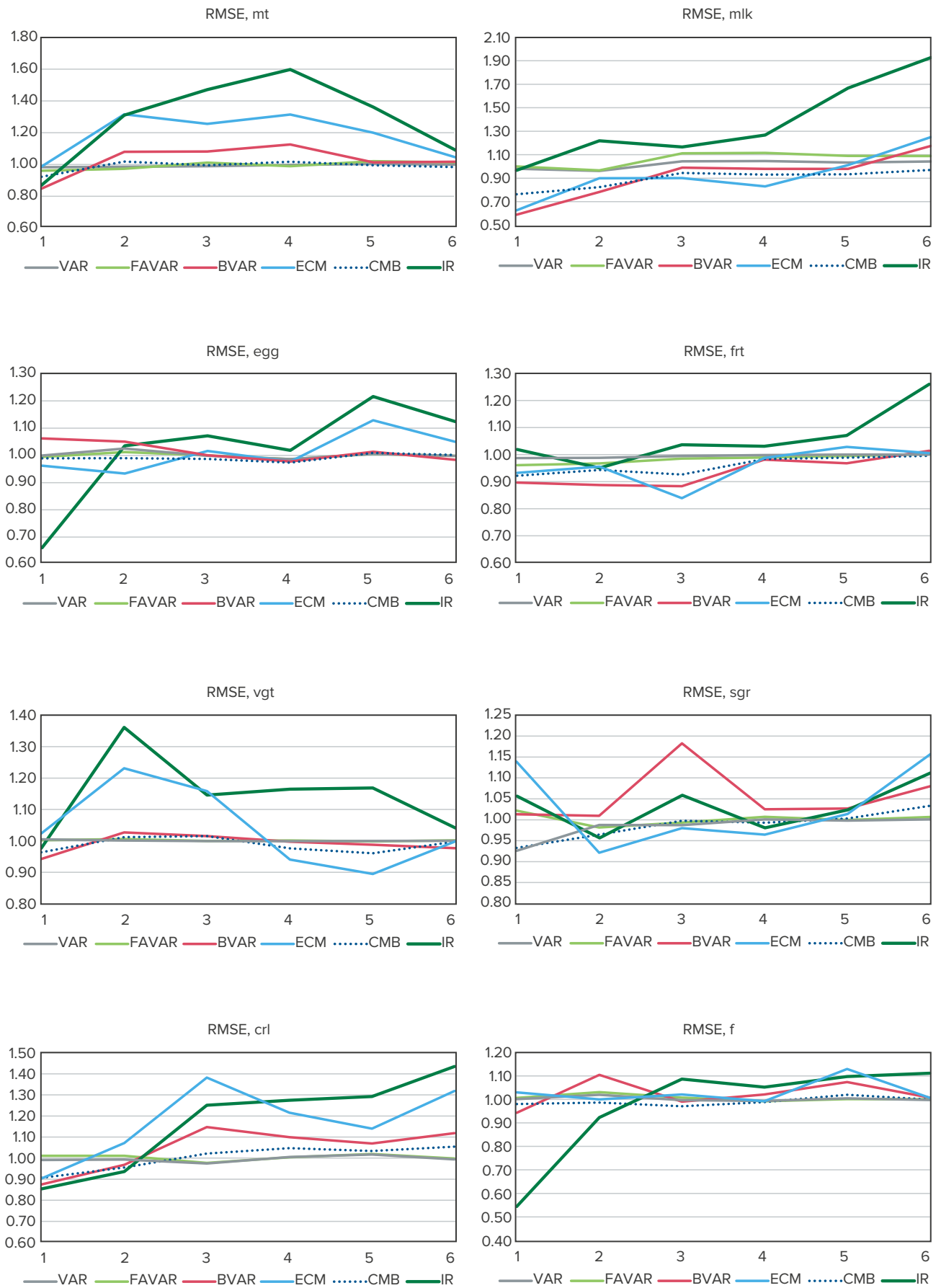


Figure B.4. RMSE, Relative to AR's Model RMSE, the RFPI

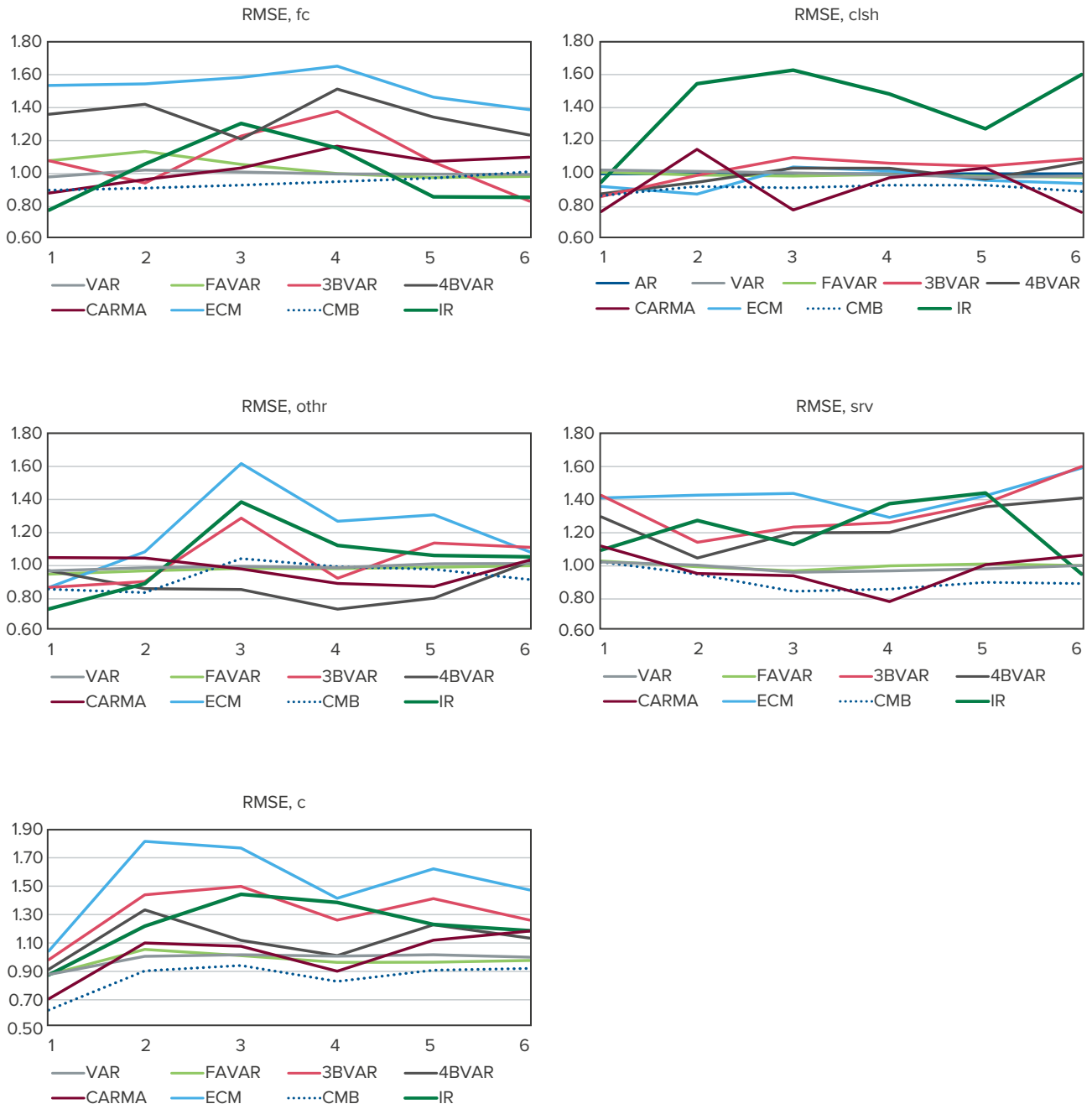


Figure B.5. RMSE, Relative to AR's Model RMSE, core CPI

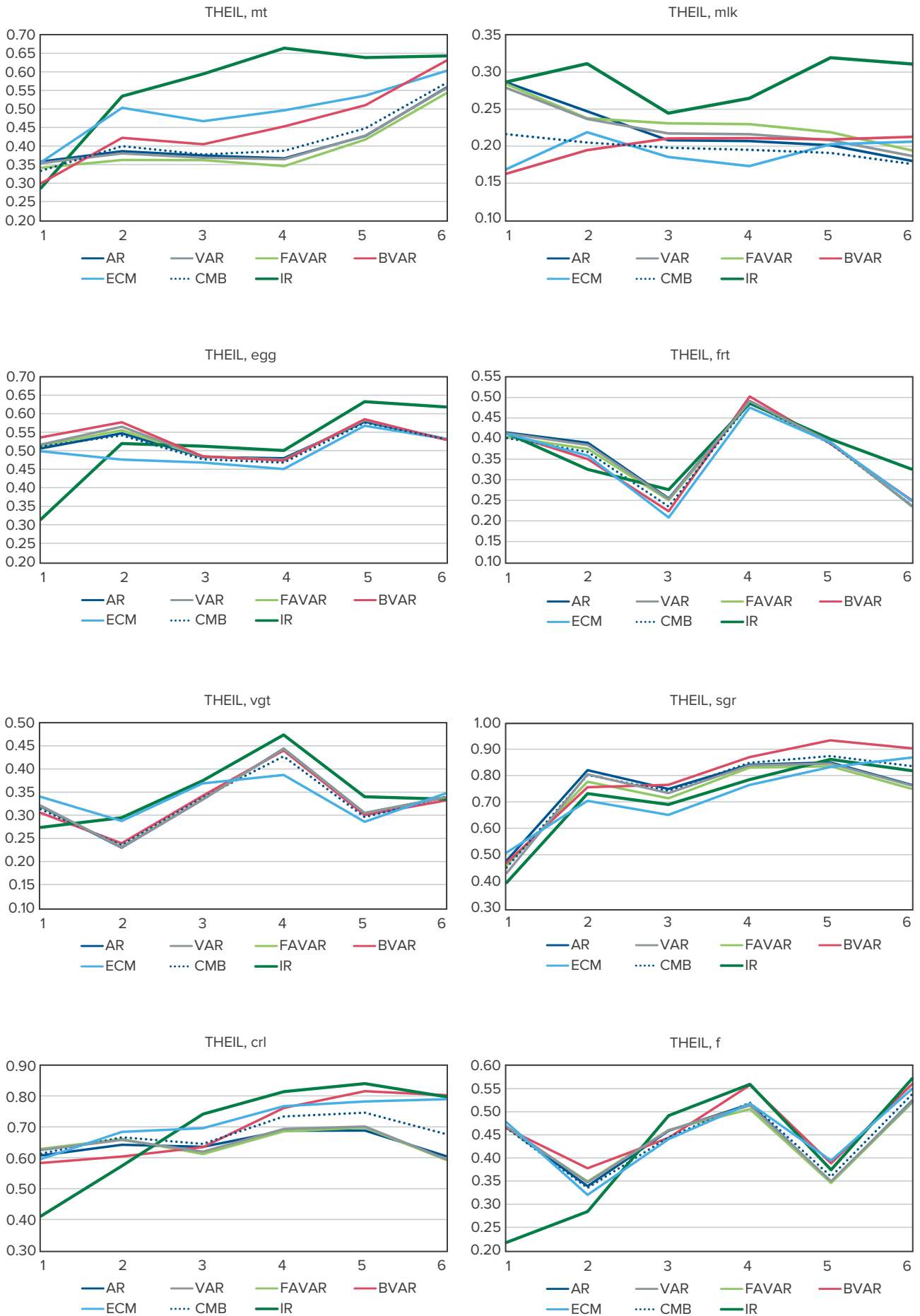


Figure B.6. Theil Index, the RFPI

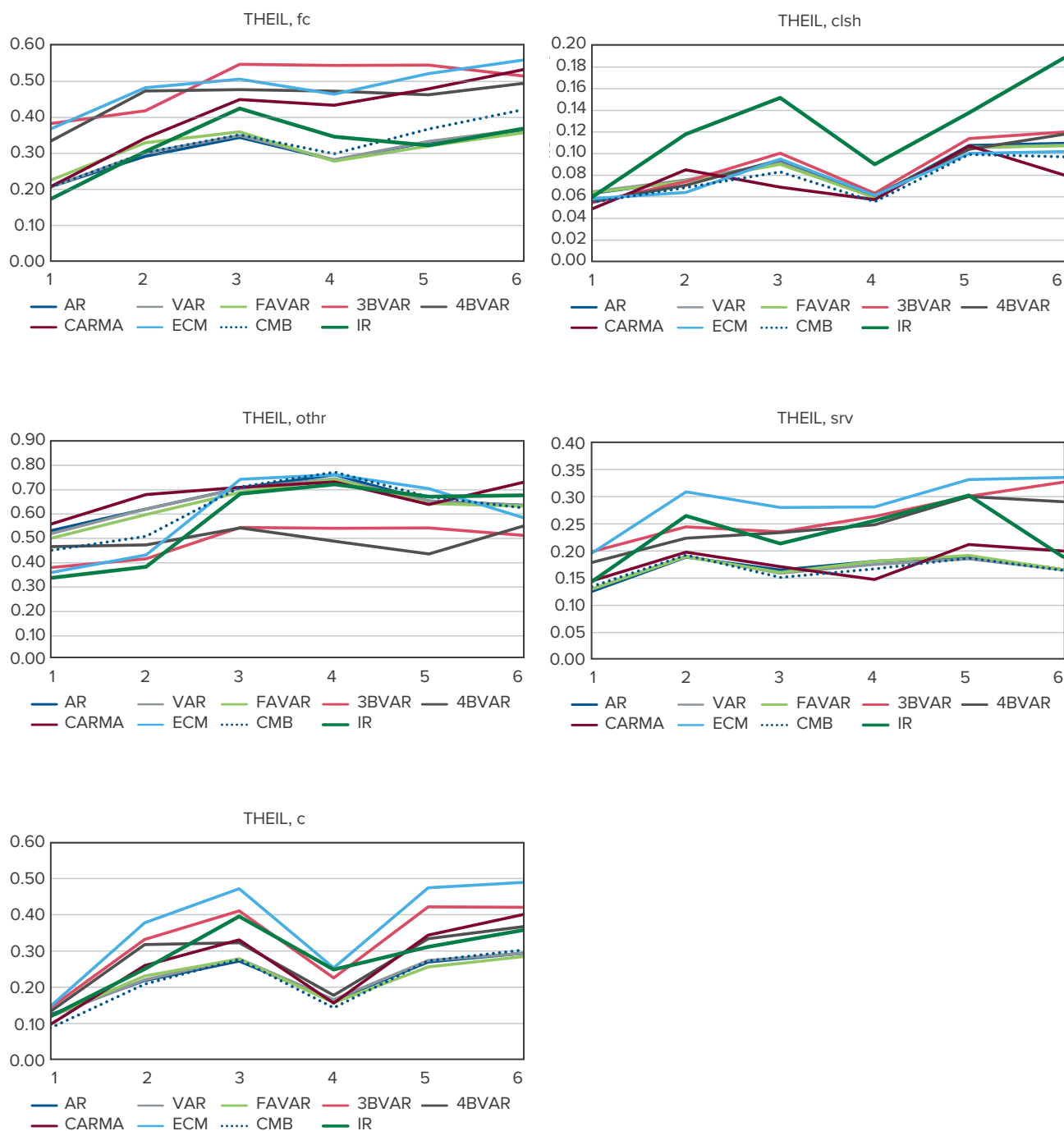


Figure B.7. Theil Index, core CPI

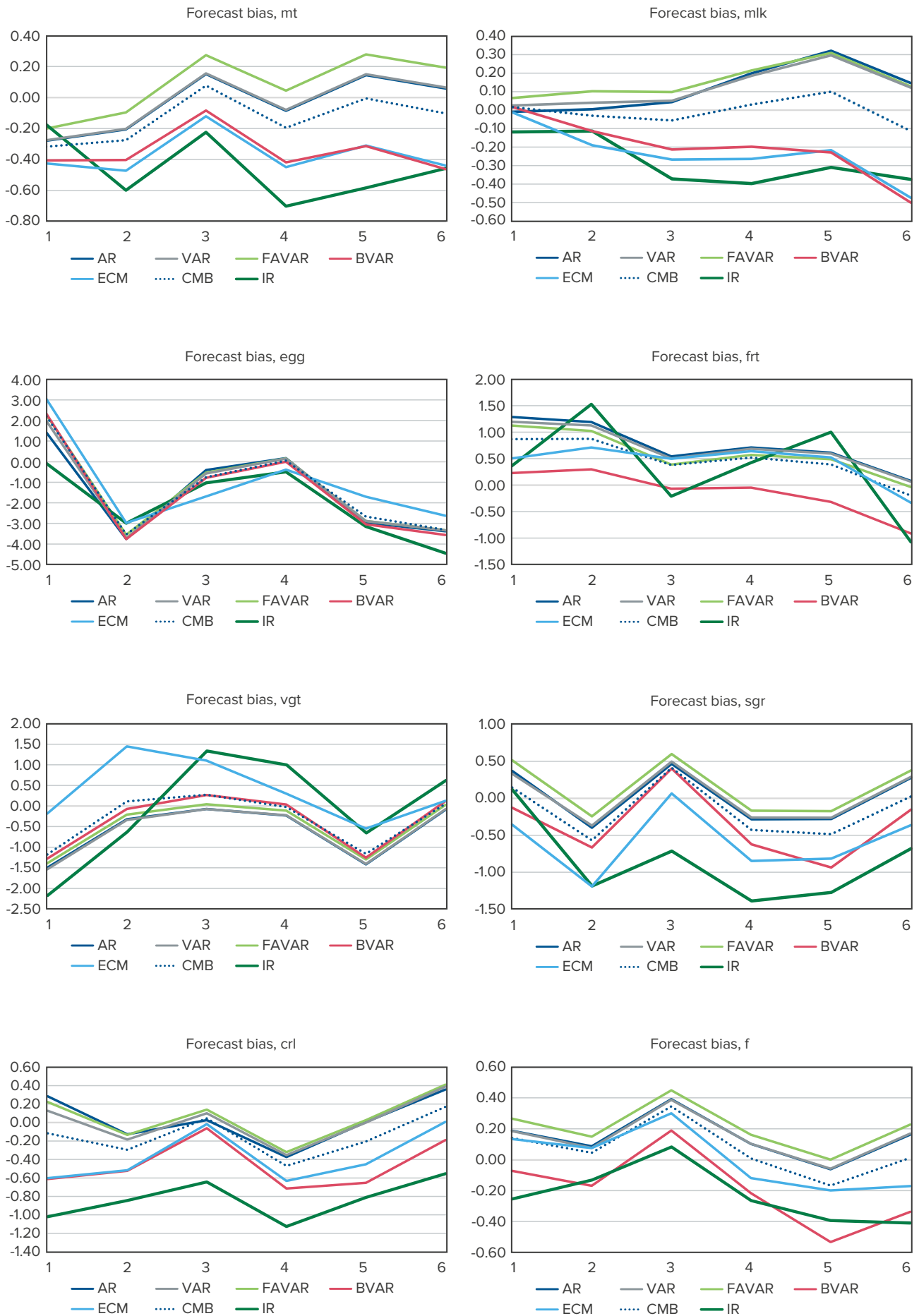


Figure B.8. Forecast Bias, the RFPI

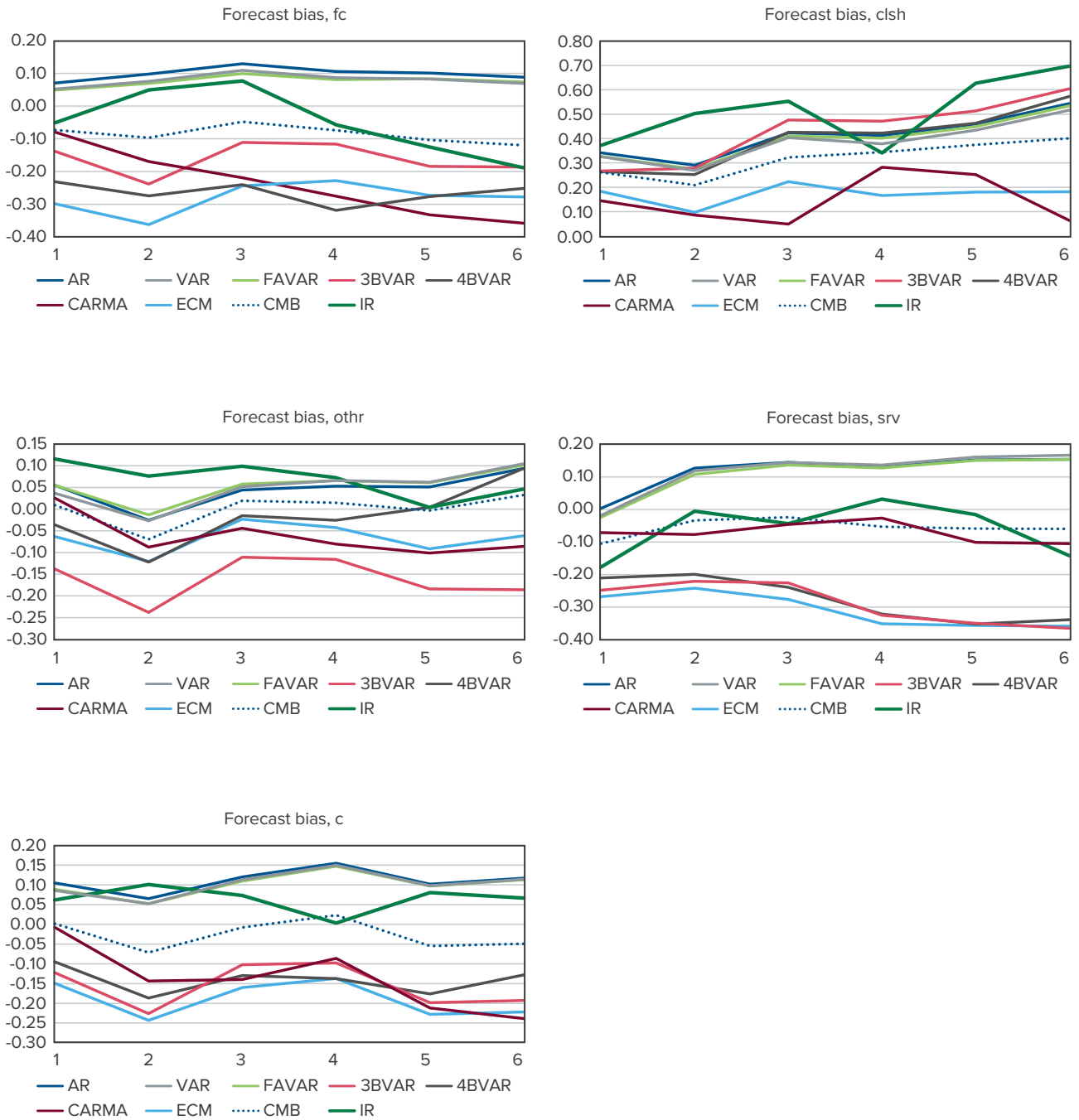


Figure B.9. Forecast Bias, core CPI

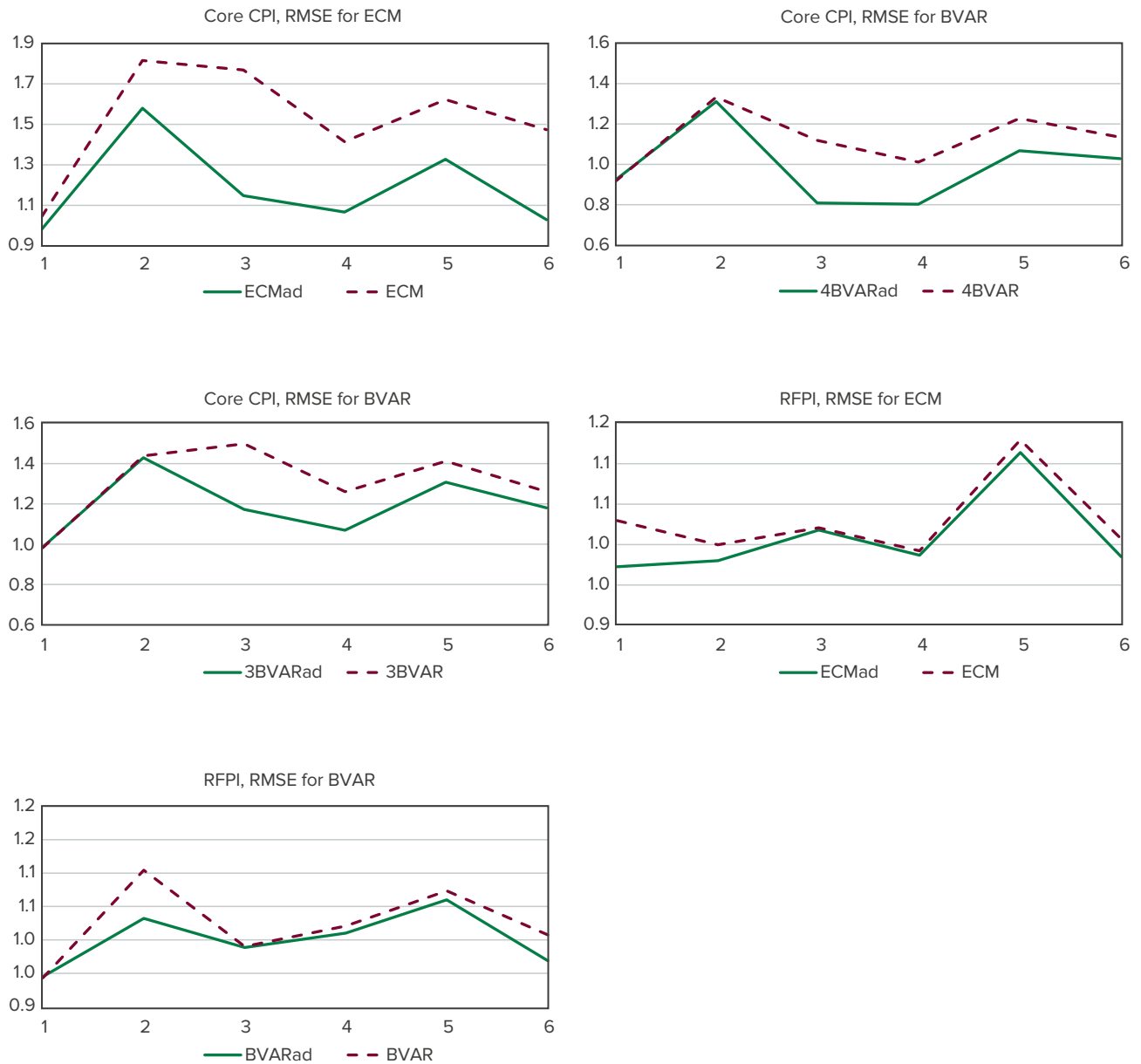


Figure B.10. RMSE, Relative to AR's Model RMSE (models with assumptions and actual data)

Note: ad stands for actual data for exogenous variables instead of assumptions.